



**INO-CNR**  
ISTITUTO  
NAZIONALE DI  
OTTICA

# Infrared digital holography with a quantum cascade laser

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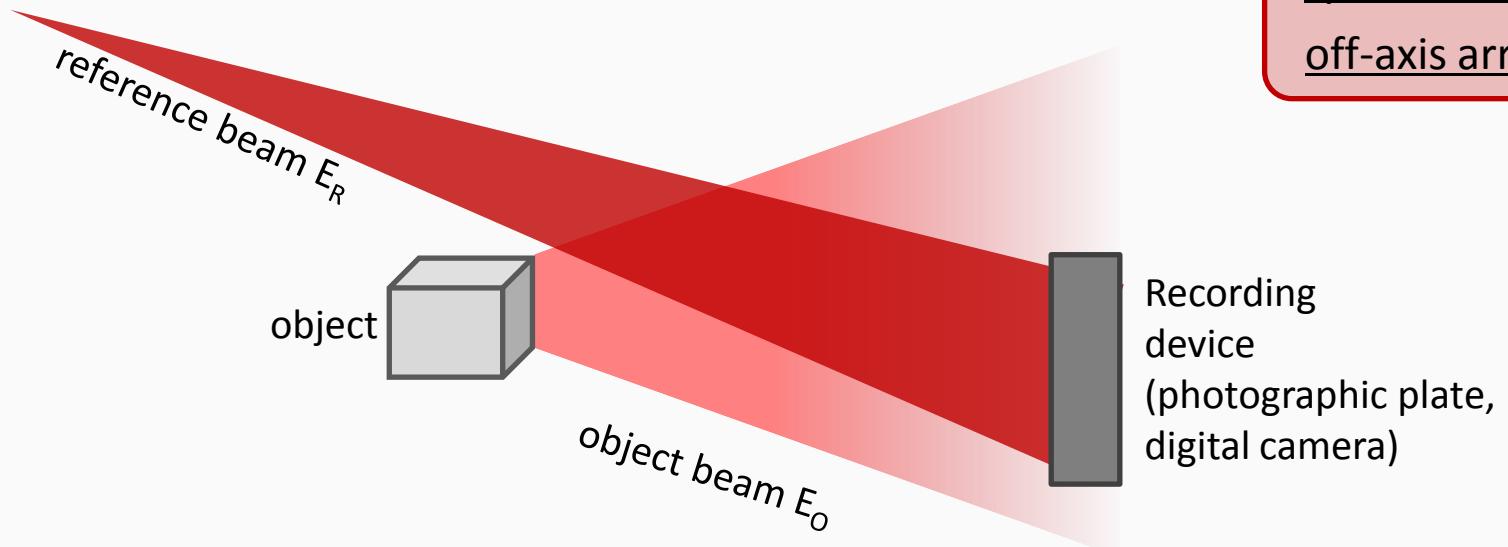
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# Outline

- **Infrared digital holography**
  - Analog/Digital hologram reconstruction
  - Long wavelength holography
- **Mid-IR QCL based holography**
  - Experimental setup and results
  - Holographic interferometry
- **THz QCL based holography**
  - Experimental setup and preliminary results
- **Conclusion**

# Hologram recording



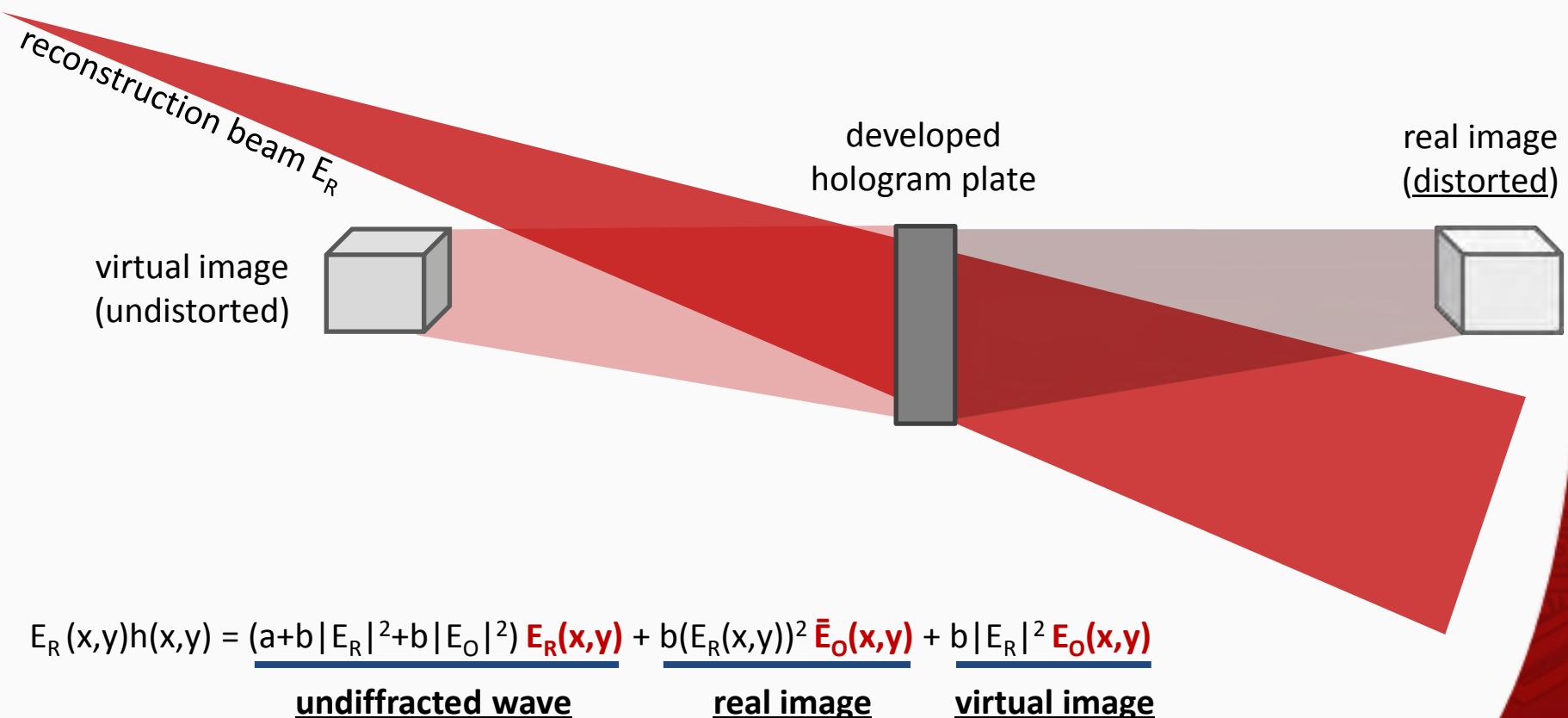
speckle holography  
off-axis arrangement

$$\text{Recorded intensity } I(x,y) = |E_O(x,y) + E_R(x,y)|^2$$

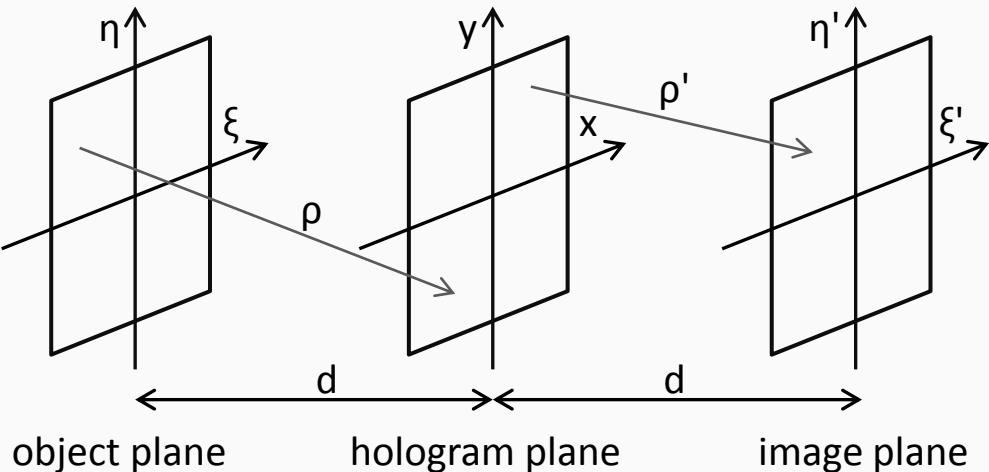
$$\text{Plate transmission } h(x,y) = a + b |E_O(x,y) + E_R(x,y)|^2$$

# Hologram reconstruction

## Analog holography



# Hologram reconstruction



Digital holography

$$\Gamma(\xi', \eta') = -\frac{i}{\lambda} \iint h(x, y) E_R(x, y) \frac{e^{ik\rho'}}{\rho'} dx dy$$

Kirchhoff diffraction integral

$$\Gamma(\xi', \eta') = -\frac{ie^{ikd}}{\lambda d} \iint h(x, y) E_R(x, y) \exp \left\{ \frac{ik}{2d} [(\xi' - x)^2 + (\eta' - y)^2] \right\} dx dy$$

Fresnel approximation

$$v = \frac{\xi'}{\lambda d} \quad \mu = \frac{\eta'}{\lambda d}$$

$$\Gamma(v, \mu) = -\frac{ie^{ikd} e^{i\pi\lambda d(v^2 + \mu^2)}}{\lambda d} \times \mathcal{F} \left\{ h(x, y) E_R(x, y) \exp \left[ \frac{ik}{2d} (x^2 + y^2) \right] \right\}$$

Fourier Transform

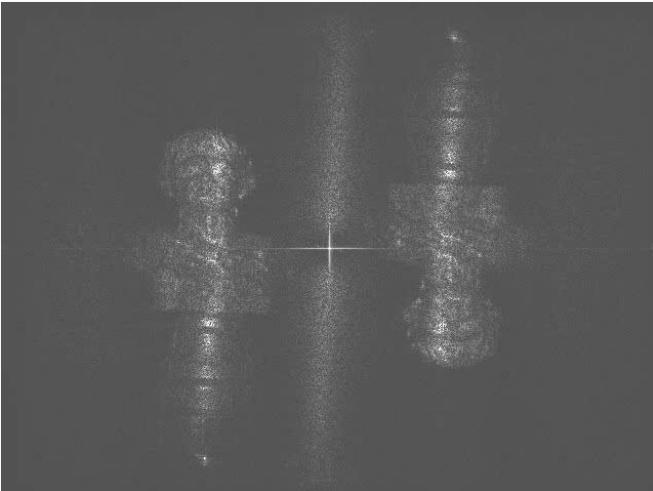
The acquired hologram is a 2D matrix  $h(m, n)$  → calculation of a DFT

# Infrared digital holography

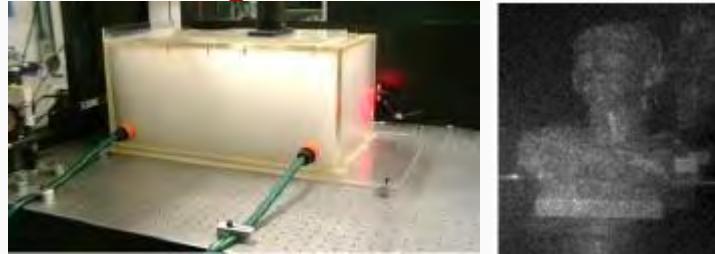
## Long wavelength acquisition

- reduced sensitivity to vibrations
- large field of view (scales with  $\lambda$ )
- high resolution
- reduced sensitivity to scattering
- use of CO<sub>2</sub> lasers

## Dynamic scene recording

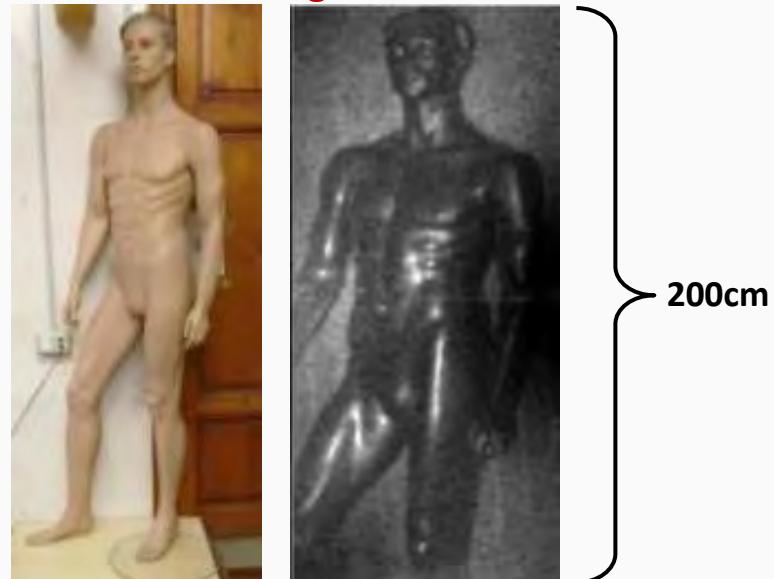


## Vision through smoke



M. Locatelli et al., Opt. Express (2013).

## Human size holograms



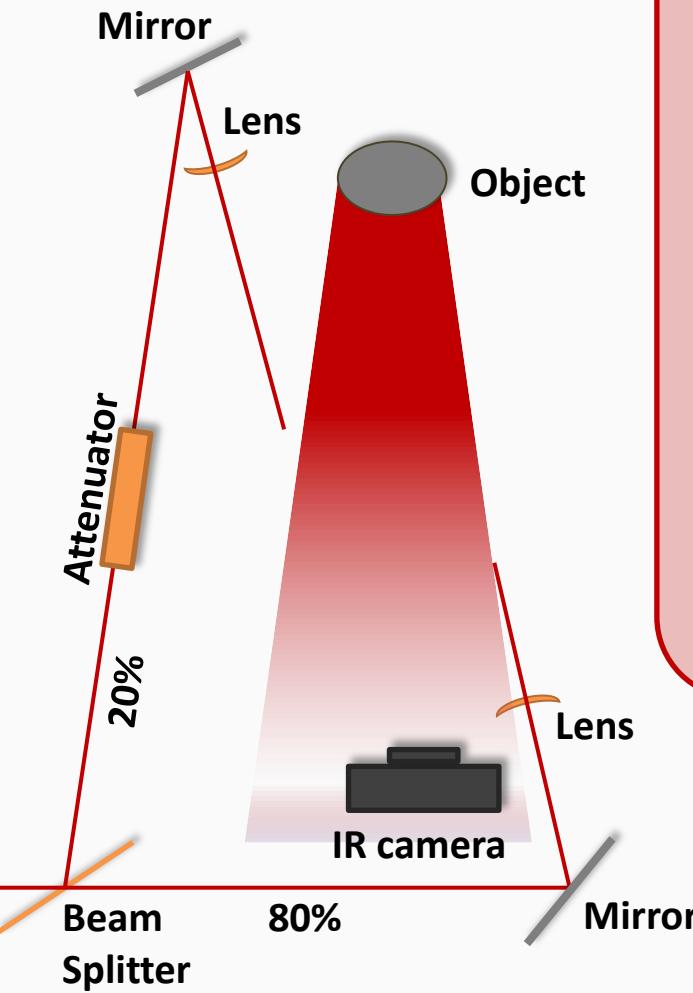
A. Pelagotti et al., J. Disp. Technol. (2010).

Use of a mid-IR QCL instead of a CO<sub>2</sub> laser? And a Terahertz QCL?

# QCL based mid-IR digital holography

## Quantum cascade laser

- Daylight solution ECqcL
- Wavelength =  $8\mu\text{m} \pm 350\text{nm}$
- Linewidth  $\leq 100\text{ MHz}$
- Output power (CW)  $\approx 80\text{mW}$
- $\text{TEM}_{00}$  beam, div  $\leq 5\text{mrad}$



## Bolometric camera

- Miricle 307K
- $640 \times 480$  pixel
- Pixel pitch  $25\text{ }\mu\text{m}$
- Sensitivity  $\leq 50\text{mK}$



# QCL based mid-IR digital holography

## Experimental results

10 cm



bronze statue



640 x 480 hologram  
frame rate 25 Hz



reconstructed  
amplitude image

$$|\Gamma(\xi, \eta')|$$

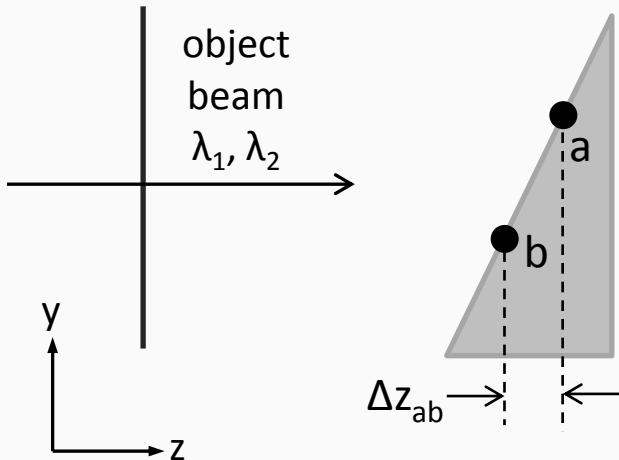
- no table vibration damping during acquisition
- real time hologram processing by Fresnel method (frame rate 5 Hz)
- maximum object dimensions limited by the QCL power

# Mid-IR holographic Interferometry

## Reconstructed phase

$$\varphi(\xi',\eta') = \text{atan} \left\{ \frac{\text{Im}[\Gamma(\xi',\eta')]}{\text{Re}[\Gamma(\xi',\eta')]} \right\}$$

## Two wavelength interferometry



$$\Delta\varphi_{1,2} = 2\pi \frac{|\lambda_1 - \lambda_2|}{\lambda_1 \lambda_2} \Delta z_{ab} = 2\pi \frac{\Delta z_{ab}}{\Lambda_{12}}$$

$$\Lambda_{12} = \frac{\lambda_1 \lambda_2}{|\lambda_1 - \lambda_2|} \quad \text{Synthetic wavelength}$$

$$\Delta z_{\text{noise}} = \Lambda \times \Delta\varphi_{\text{noise}} / 2\pi \quad \text{noise amplification}$$

### Analog holographic interferometry

Multiple exposures of the same photographic plate at different  $\lambda$

### Digital holographic interferometry

Subtraction of the reconstructed phase of distinct holograms

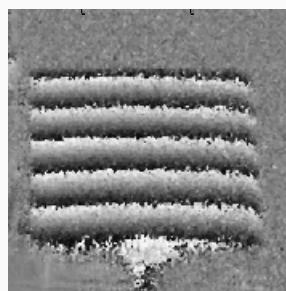
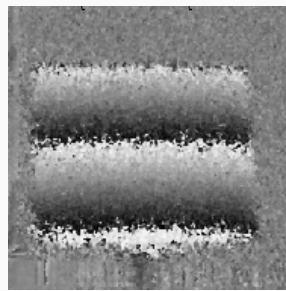
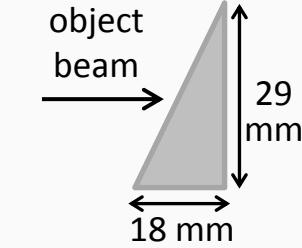
### HI with a tunable laser diode

- Adjustement of the synthetic wavelength to the optical path length to be measured  
no need for phase-unwrapping
- Possible hierarchical phase unwrapping based on progressive synthetic wavelengths:  
high dynamic range and low noise



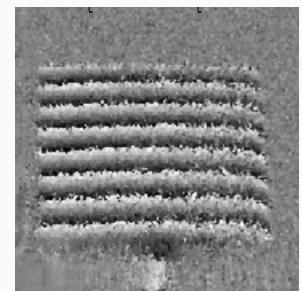
# Mid-IR holographic Interferometry

## Wedge contouring

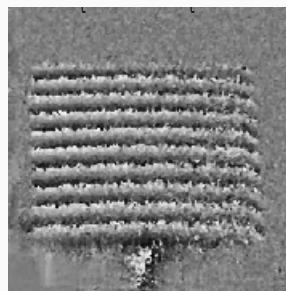


$\Lambda = 5.0 \text{ mm}$

$\Lambda = 3.4 \text{ mm}$



$\Lambda = 2.6 \text{ mm}$



$\Lambda = 2.1 \text{ mm}$

## 50L coin amplitude and phase



amplitude



$\Lambda = 10.0 \text{ mm}$



$\Lambda = 5.0 \text{ mm}$



$\Lambda = 3.3 \text{ mm}$



$\Lambda = 2.5 \text{ mm}$



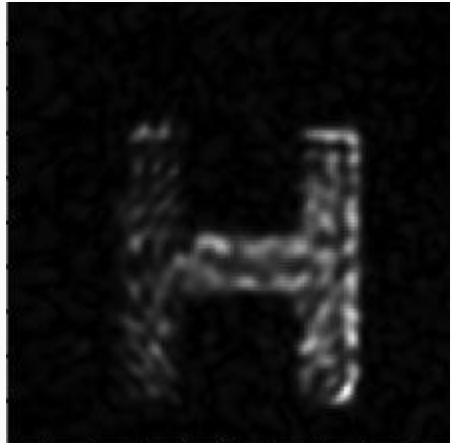
$\Lambda = 2.0 \text{ mm}$

ECqcL → synthetic wavelength range from 100s  $\mu\text{m}$  to  $\approx 20 \text{ mm}$

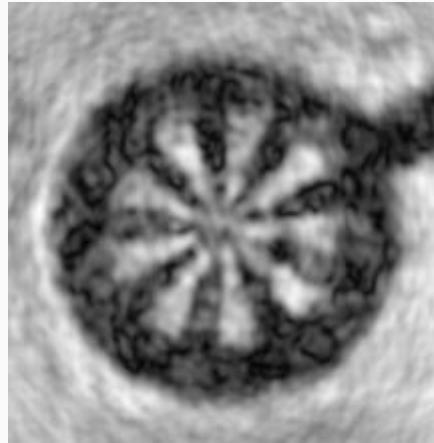
# THz Digital Holography

## Key features

- reduced sensitivity to vibrations
- large field of view
- reduced sensitivity to scattering
- high resolution
- properties of THz radiation



S. Ding et al. Opt. Lett. (2011)



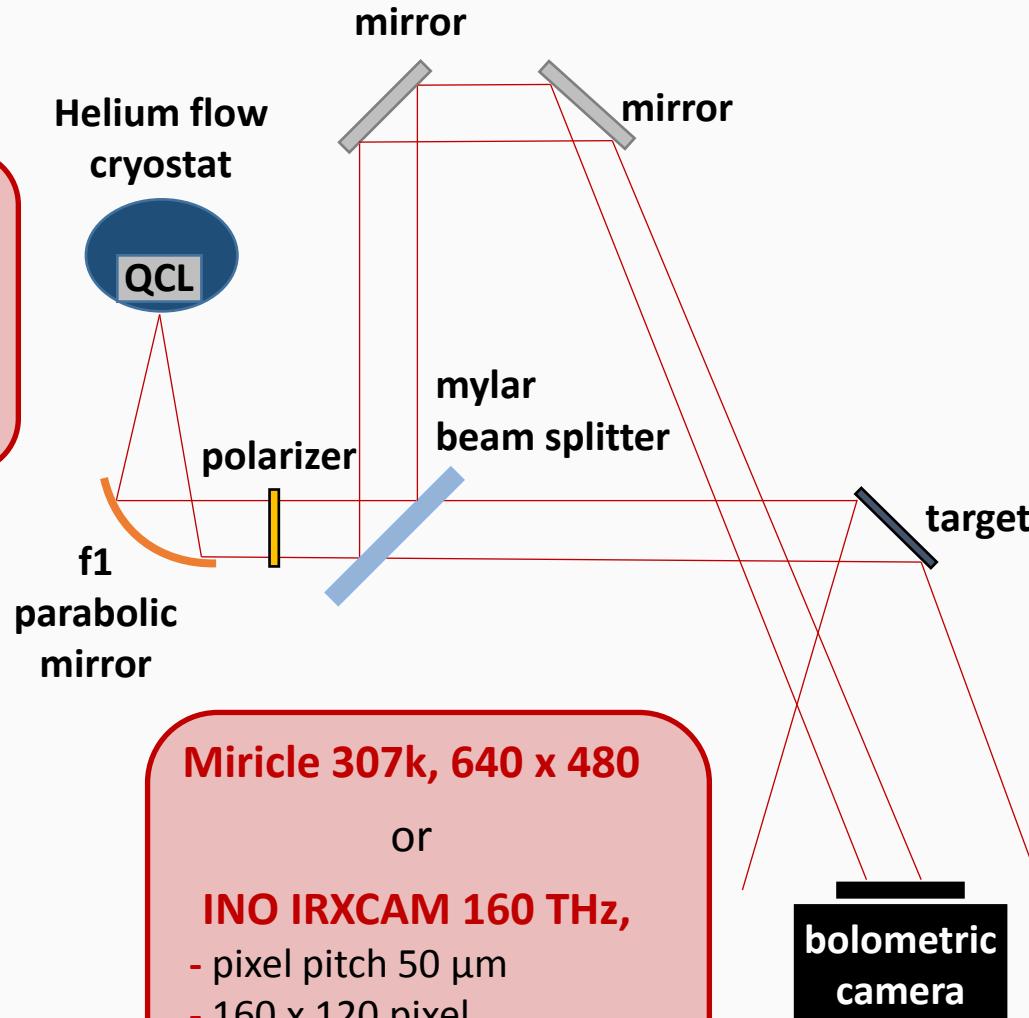
E. Hack et al., Opt. Express (2013)

# Digital Holography with a THz QCL

## Experimental setup

### Terahertz QCL

- bound to continuum
- single plasmon waveguide
- $T = 20 \text{ K}$
- output power 4 mW



Miricle 307k, 640 x 480

or

INO IRXCAM 160 THz,

- pixel pitch 50  $\mu\text{m}$
- 160 x 120 pixel
- NEP 100 pW

bolometric  
camera

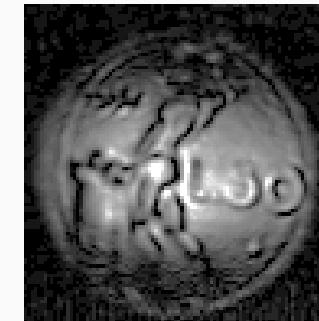
# Digital Holography with a THz QCL

## Preliminary results

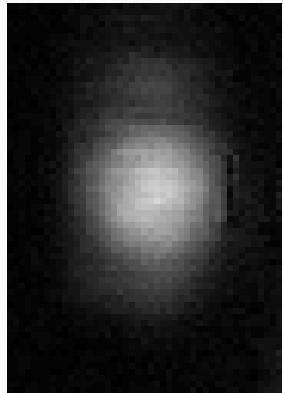
### Small button



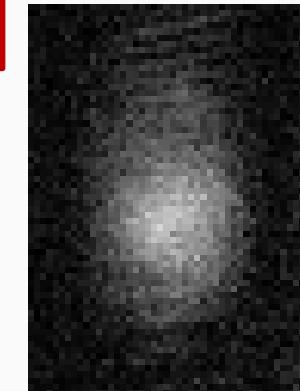
### 50 Lire coin



### Moving target



... behind 1mm black Polypropylene plate



Speed = 10mm/s

# Conclusions

## ➤ **Digital holography based on Mid-IR QCLs**

- Compact setup for IR DH
- Coverage of a broad Mid-IR spectrum (3-16  $\mu\text{m}$ )
- Use of external cavity QCLs for versatile path length measurements

## ➤ **Digital holography based on terahertz QCLs**

- First demonstration of speckle digital holography
- Work in progress: holography of biological samples, non destructive analysis, THz path length measurements