

Microwave modulation of quantum cascade lasers

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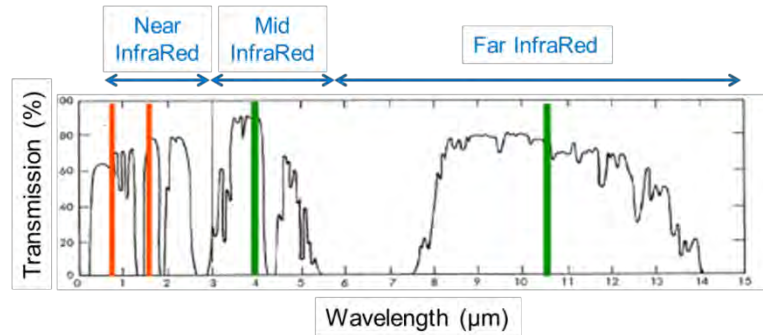
European Research Council
Executive Agency

ADEQUATE



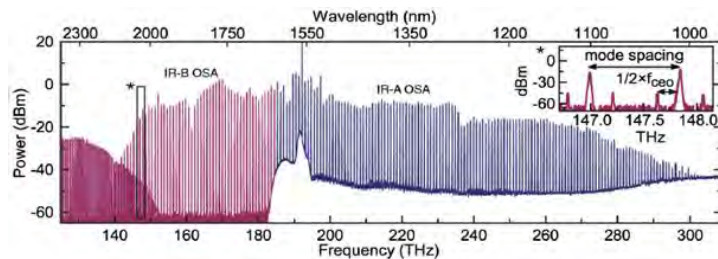
Motivations for high frequency modulation

- Free space communications

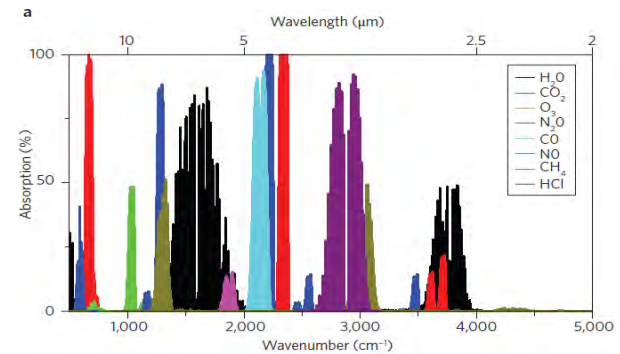


High resolution and high sensitivity spectroscopy

- Frequency combs

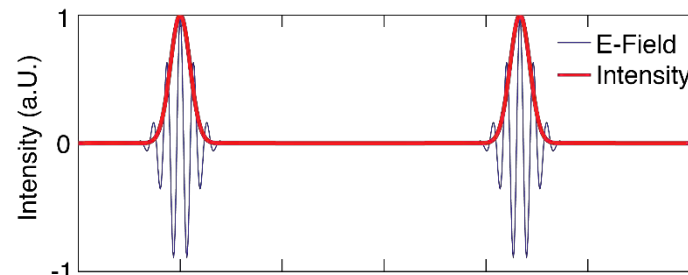


P. Del'Haye, et al., *Physical Review Letters* **107** 063901 (2011)



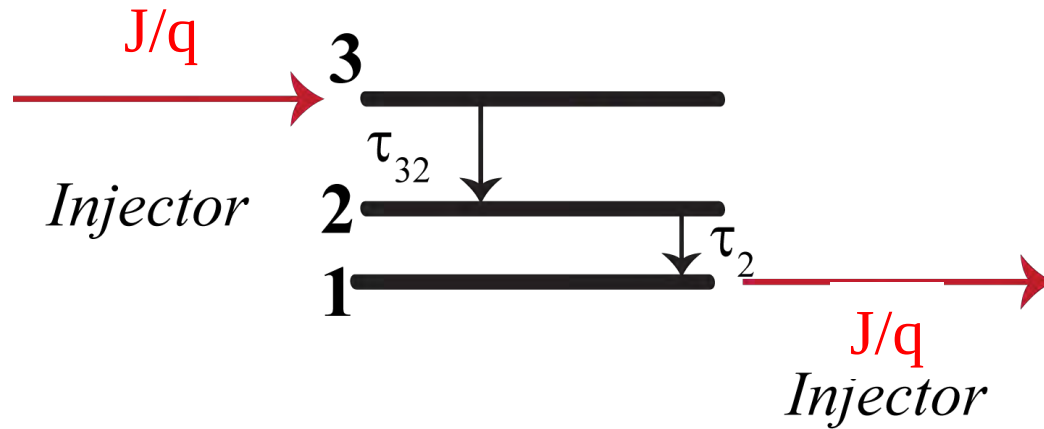
A. Schliesser, et al., *Nature Photonics* **6** 440-449 (2012)

- Mode locking



Ultrafast unipolar optoelectronics

Rate equation analysis



$$\frac{1}{\tau_3} = \frac{1}{\tau_{31}} + \frac{1}{\tau_{32}}$$

$$\frac{dn_3}{dt} = \frac{J}{q} - \frac{n_3}{\tau_3} - Sg_c(n_3 - n_2)$$

~~$$\frac{dn_2}{dt} = \frac{n_3}{\tau_{32}} - \frac{n_2}{\tau_2} + Sg_c(n_3 - n_2)$$~~

$$\tau_2 = 0 !$$

$$\frac{dS}{dt} = \left(g_c(n_3 - n_2) - \frac{c\alpha_{tot}}{n_o} \right) S + \beta \frac{n_3}{\tau_{sp}}$$

Small amplitude analysis

Small signal approximation

$$\begin{aligned} S(t) &= S^{(0)} + \mathbf{S}e^{i\omega t} \\ J(t) &= J^{(0)} + \mathbf{J}e^{i\omega t} \\ n_i(t) &= n_i^{(0)} + \mathbf{n}_i e^{i\omega t} (i = 3, 2) \end{aligned}$$

Transfer function

photon population $\rightarrow$ $S = h(\omega) \frac{S^{(0)}}{J^{(0)}} \mathbf{J}$ $\leftarrow$ Current modulation

$$|h(\omega)|^2 = \frac{1}{1 + \omega^4 \tau_p^2 \tau_{stim}^2 + \omega^2 \tau_{stim} \tau_p \left(\frac{\tau_p}{\tau_{stim}} + 2 \frac{\tau_p}{\tau_{up}} + \frac{\tau_p \tau_{stim}}{\tau_{up}^2} - 2 \right)}.$$

$$\tau_p \approx 10\text{ps} \ (\alpha = 10\text{cm}^{-1})$$

with:

$$0.5\text{ps} < \tau_{up} < 1\text{ps}$$

$$0.1\text{ps} < \tau_{stim} < 100\text{ps}$$

J. Faist, *Quantum Cascade Lasers* (2013)

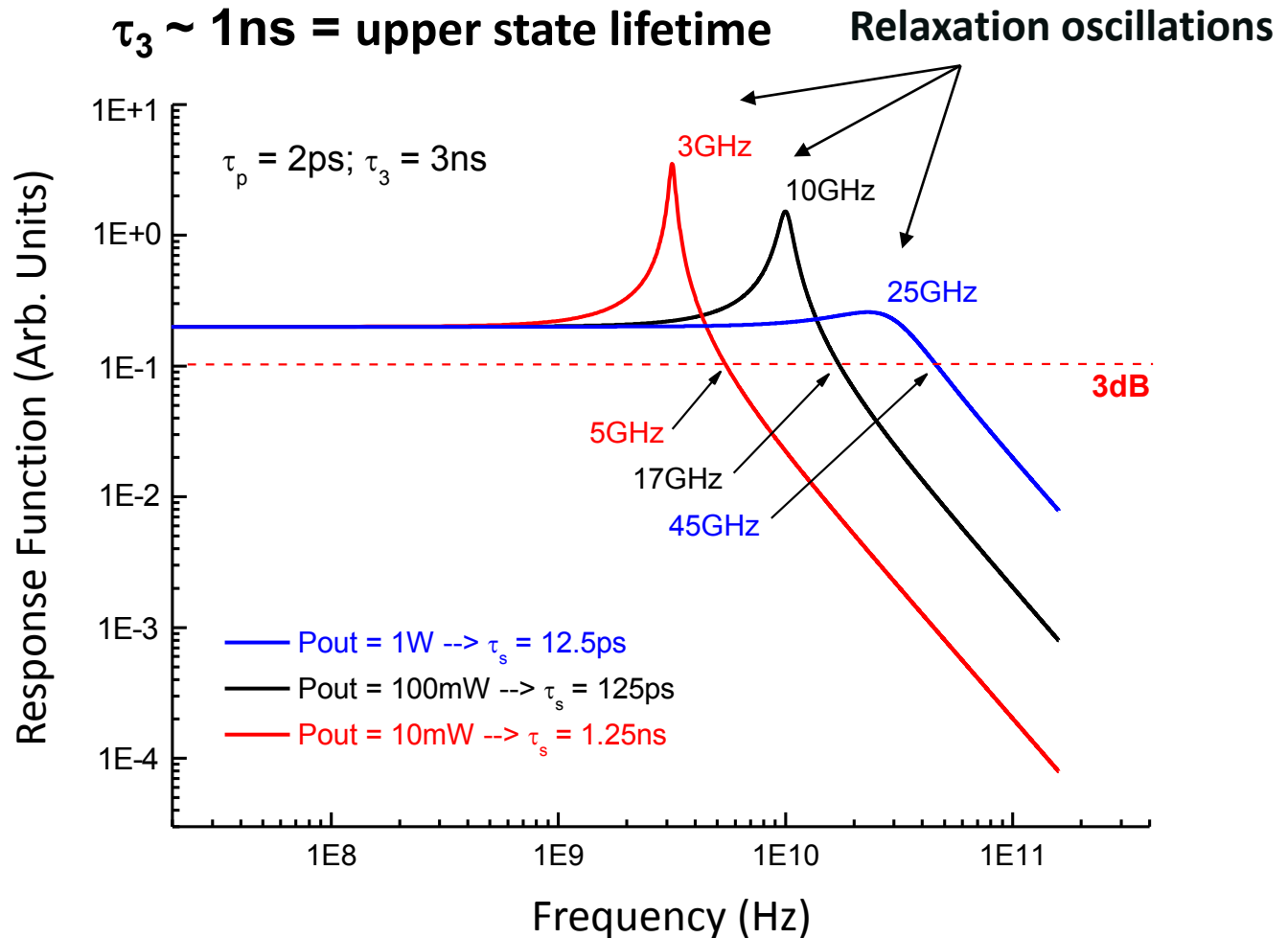
A. Yariv, *Photonics* (2007)

Frequency response function of a diode laser : $H(\omega)$

$$\delta P_{\text{opt}} = H(\omega) \delta I$$

$H(\omega)$ describe the efficiency of transferring
a current modulation into an optical modulation

$$\tau_3 \gg \tau_s > \tau_p$$



Frequency response function of QC lasers

$\tau_3 \sim 1\text{ps}$ = upper state lifetime

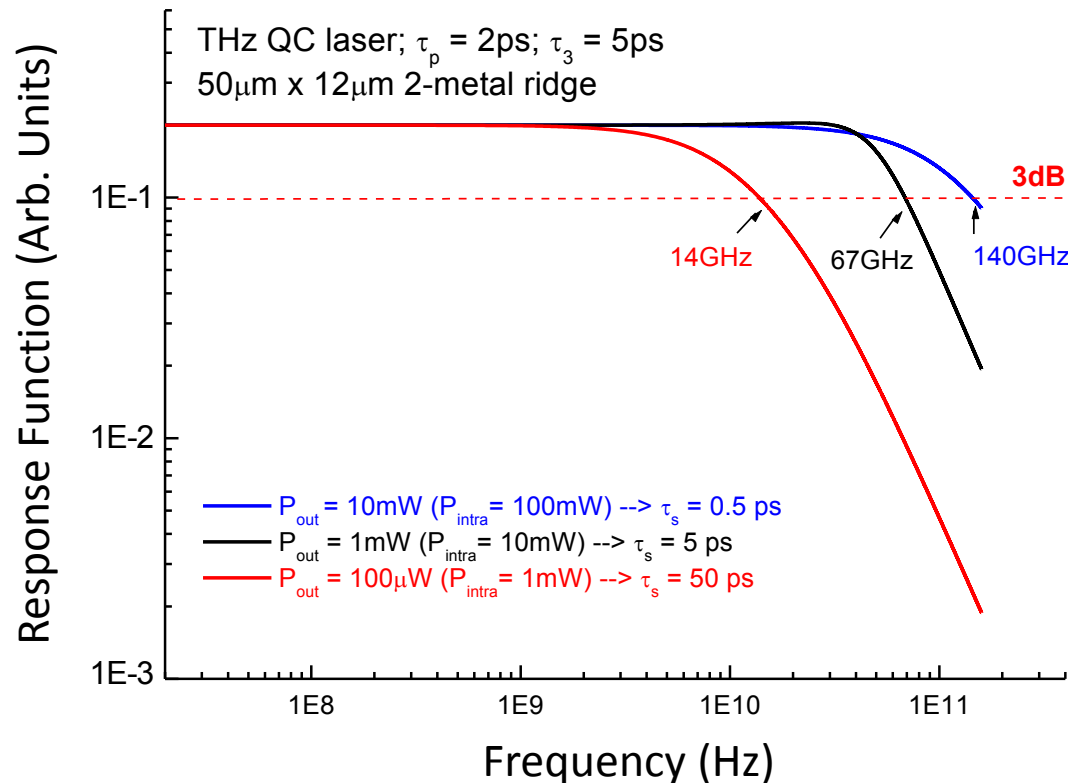
$$\tau_3 \sim \tau_s \sim \tau_p$$

➔ Short non-radiative lifetime $\sim 1\text{ps}$ ➔ no relaxation oscillations!

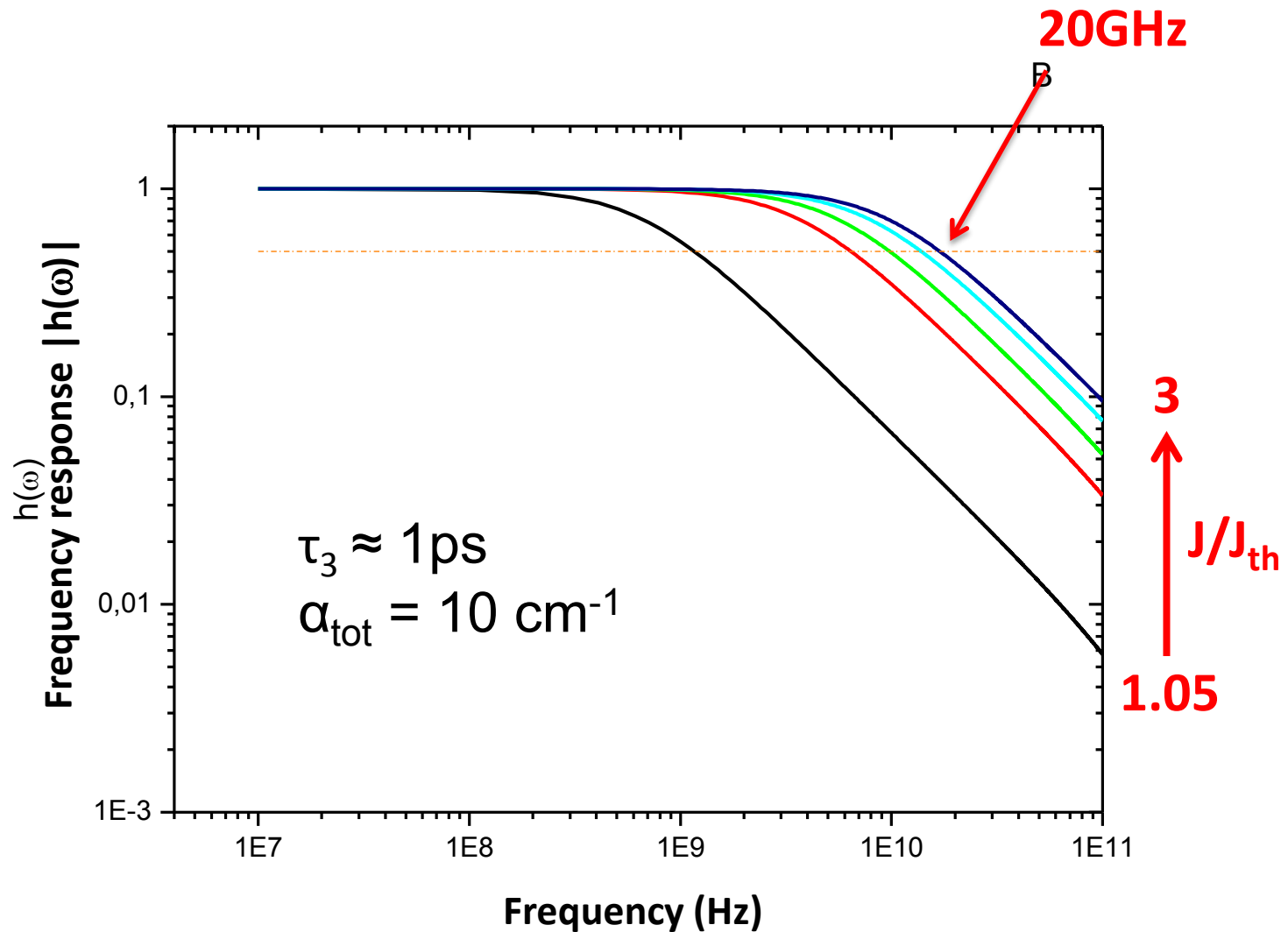
The system acts as an over-damped oscillator

➔ Short stimulated lifetime $\sim 1\text{ps}$ ➔ very wide band of modulation

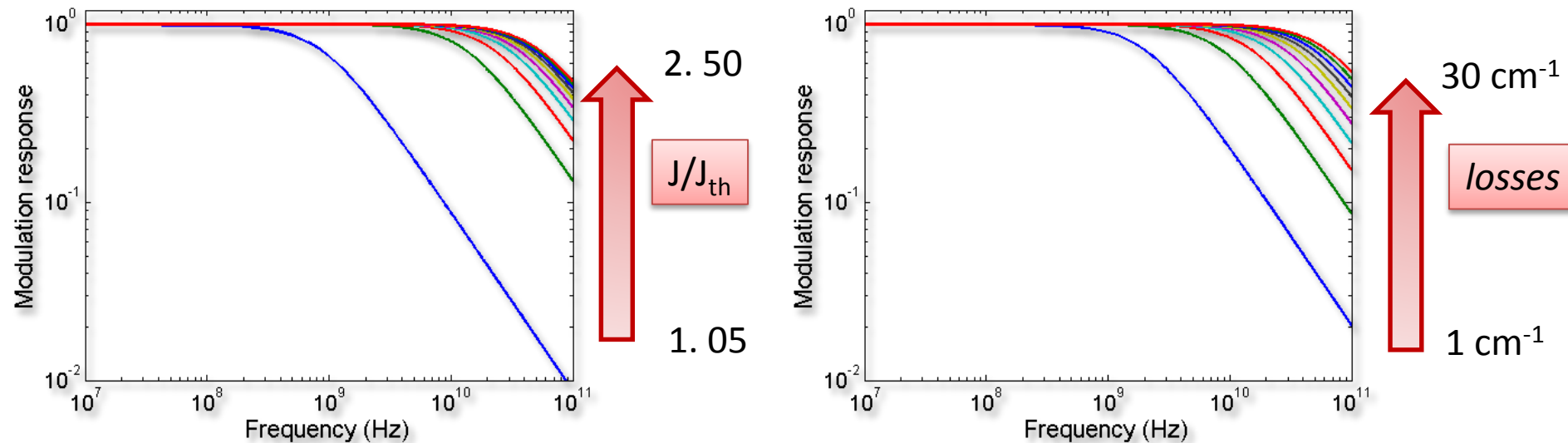
The cascade enhance the number of photon in the cavity



Calculated frequency response for a “real” QC laser



High frequency modulation band-width



For laser driven well above threshold the modulation band is

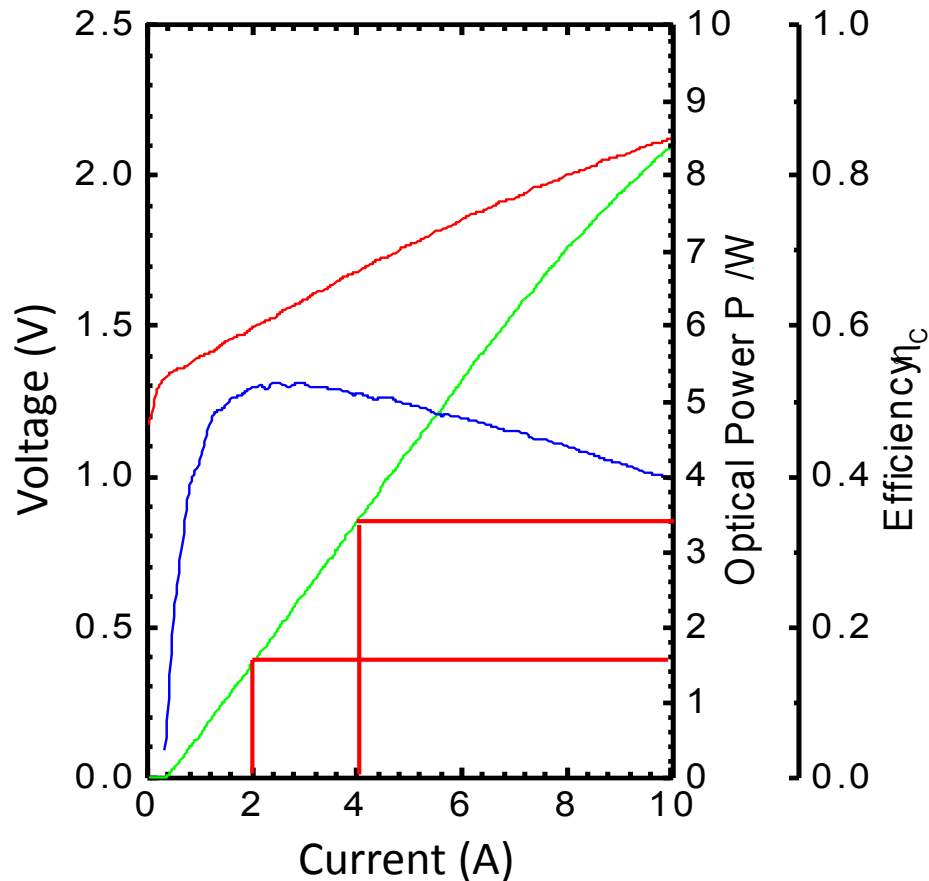
$$\Delta\omega_{Mod} \approx \frac{1}{\sqrt{\tau_{stim}\tau_p}} \quad \tau_{up} ?$$

Performance comparison between DLs and QCLs

(State-of-the-art)

$\lambda = 0.8\mu\text{m} \Rightarrow 1500\text{ meV}$

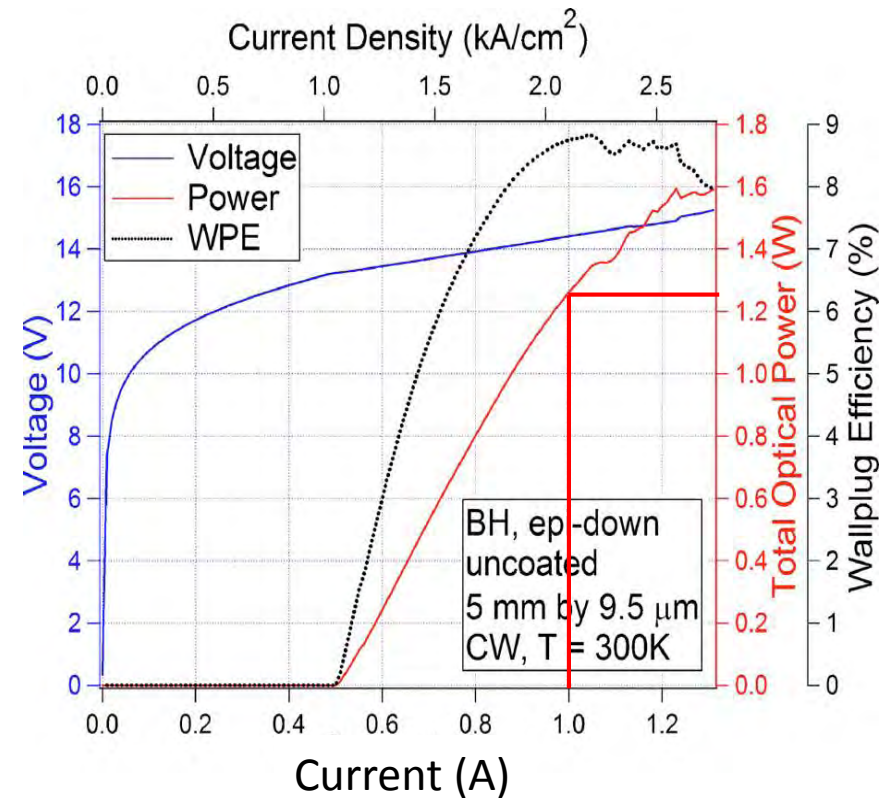
Facet surface = $100\text{ }\mu\text{m}^2$



Diode Laser

$\lambda = 5\mu\text{m} \Rightarrow 240\text{ meV}$

Facet surface = $25\text{ }\mu\text{m}^2$



QC Laser

L'effet cascade

Cascade injection

Electron recycling due to a sequence of active region in series

Threshold and slope efficiency are functions of the number (N_p) of repeated active regions

$$J_{th} = \frac{\alpha_w + \alpha_m}{g \boxed{N_p} \Gamma_p}$$

$$\frac{dP}{dI} = \frac{1}{2} \boxed{N_p} \frac{e}{h\nu} \frac{\alpha_m}{\alpha_w + \alpha_m} \left[1 - \frac{\tau_2}{\tau_{32}} \right]$$

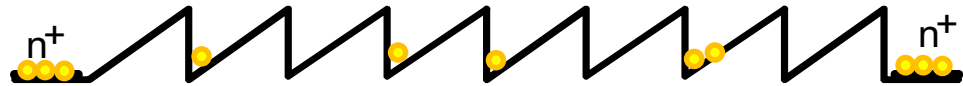
Quantum efficiency = $N_p/N_e > 1$

$$\eta_d = \frac{2e}{h\nu} \frac{dP}{dI} \sim \mathbf{10} \text{ at room temperature}$$

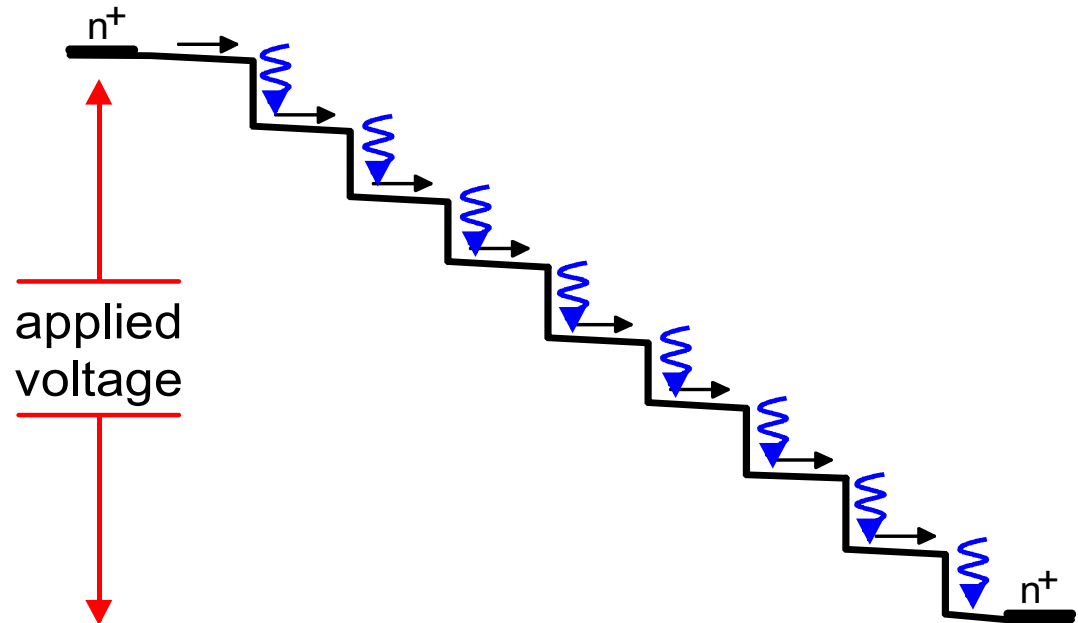
Sawtooth to staircase transition

*Electron recycling and
Trading current for voltage*

Unbiased: $V = 0$

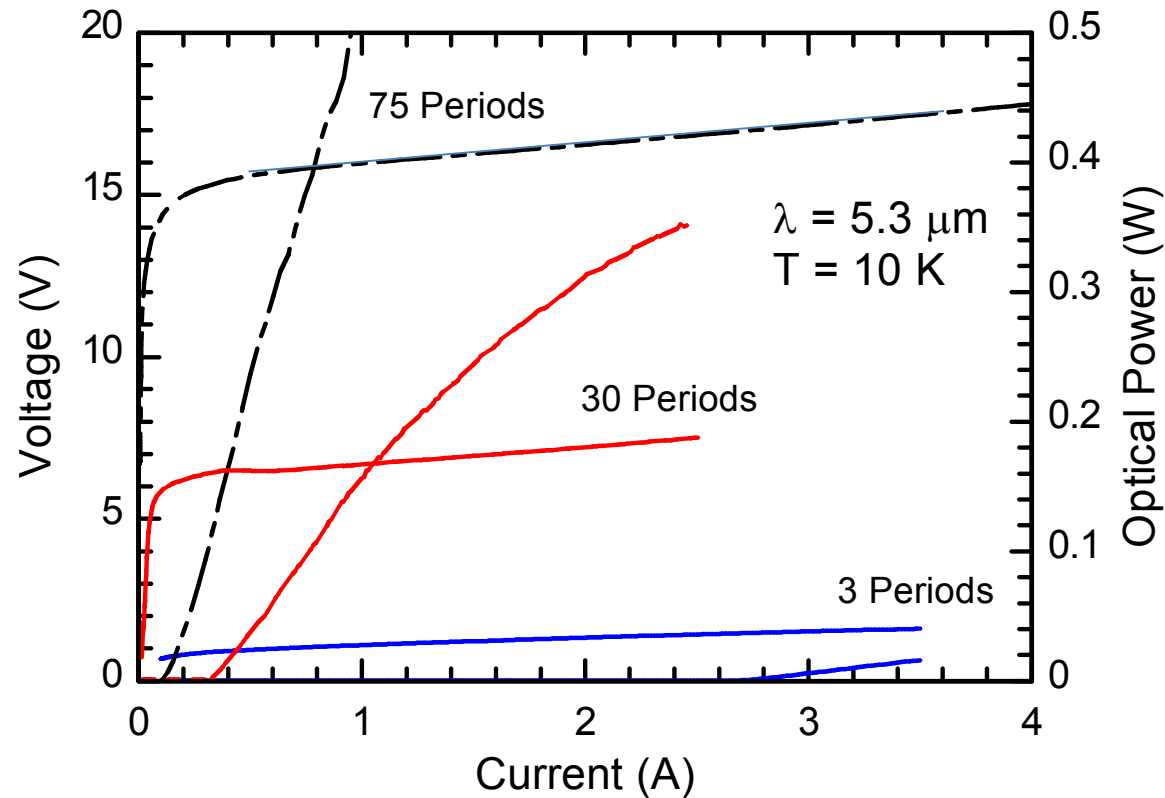


Biased: $V > V_{th}$

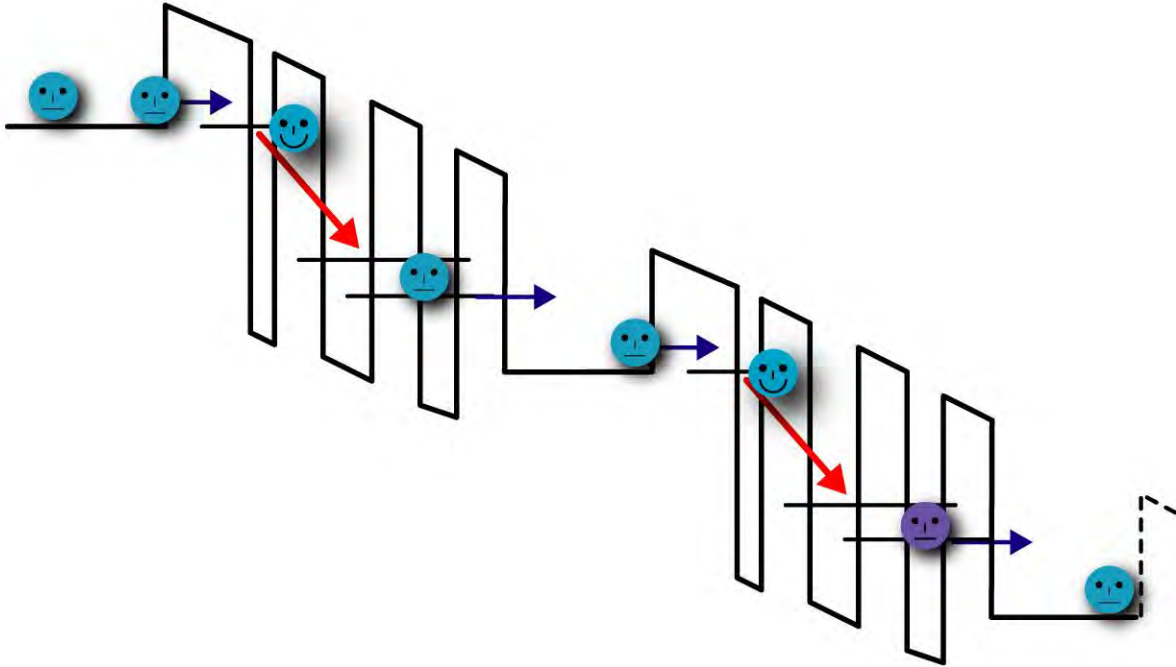


QC lasers as a function of the number of period

Experimental evidence of V-I trade

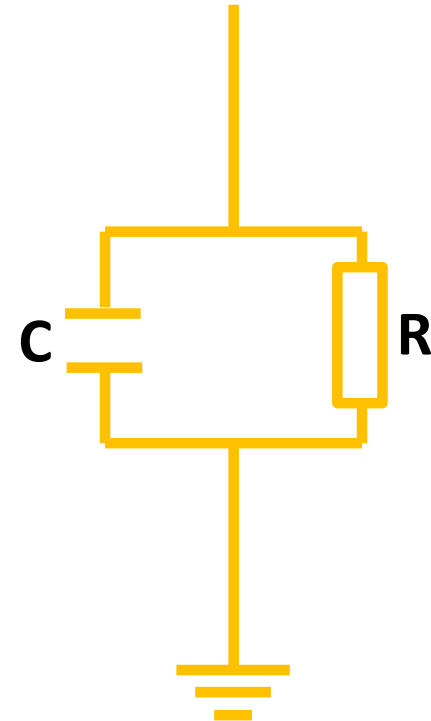
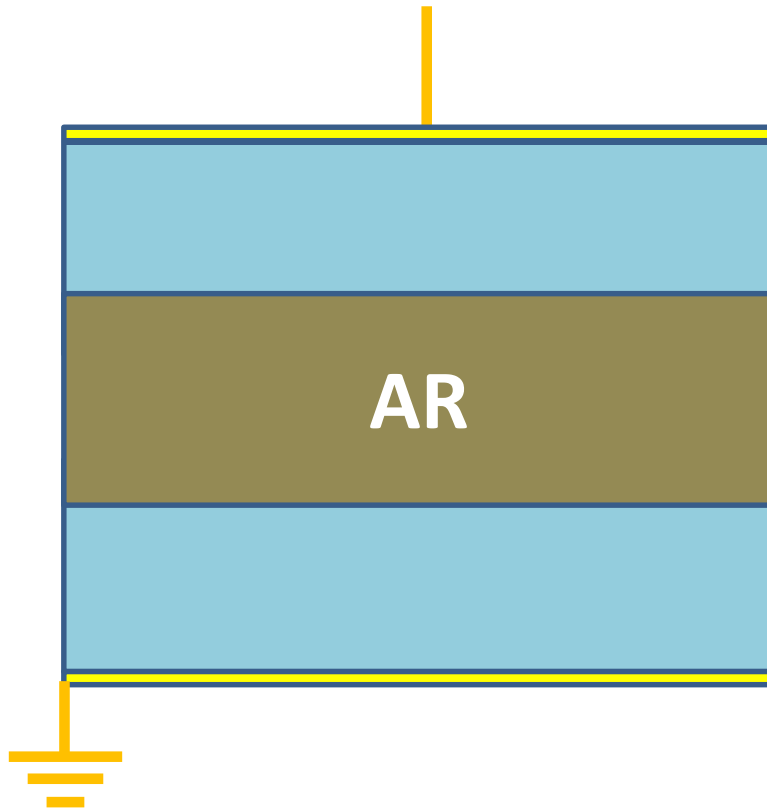


Cascade



Cascade: répétition d'une période
-> 1 électron peut générer plusieurs photons

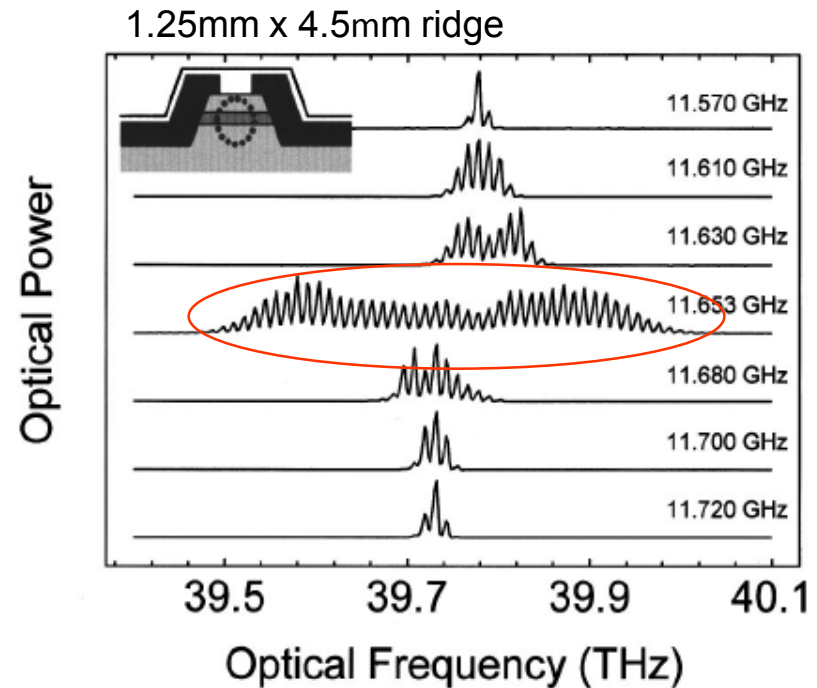
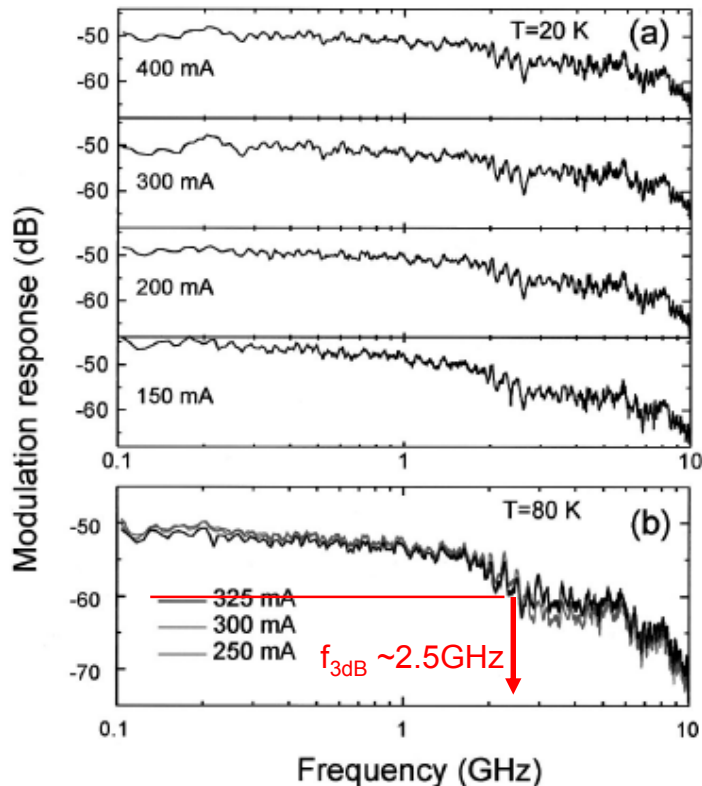
100GHz band width?



$$\omega_{cut-off} \approx \frac{1}{2\pi RC} = \frac{1}{2\pi \left(\frac{dV}{dI}\right) C} \approx 20 - 30 \text{ GHz}$$

Absence of relaxation oscillations

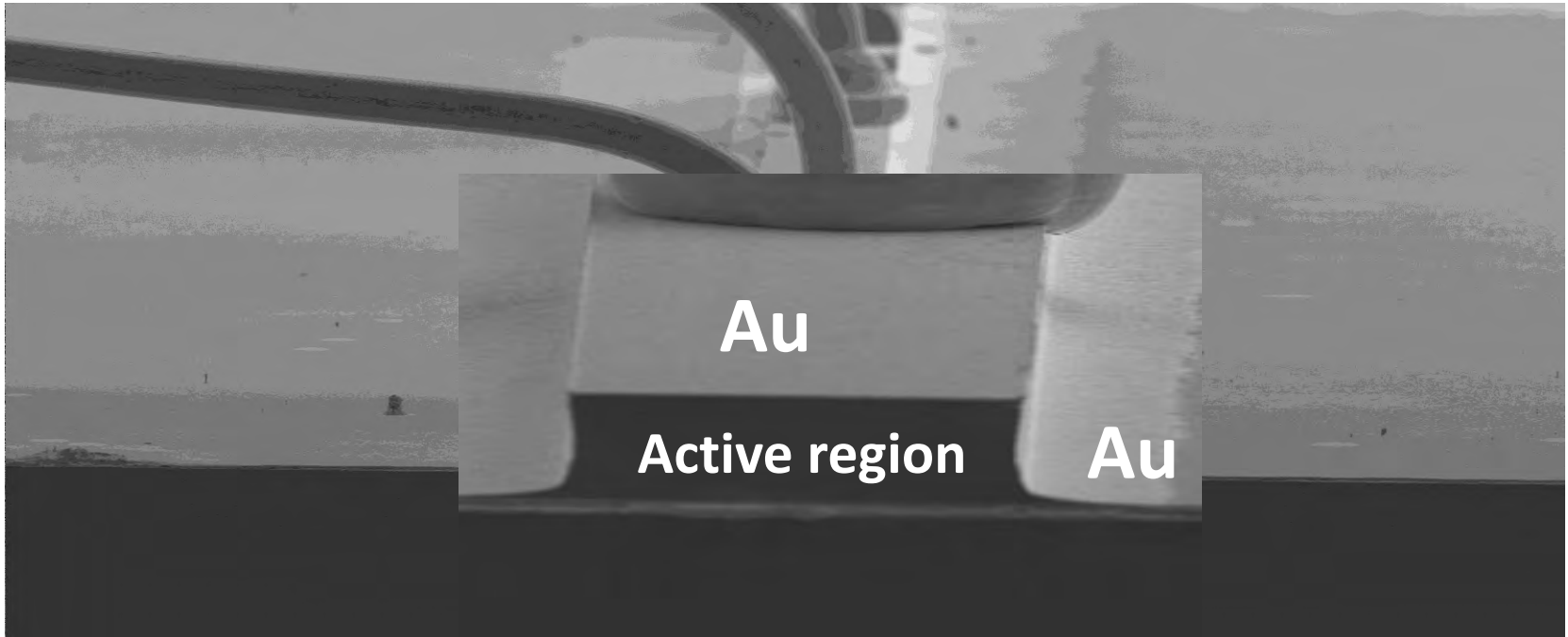
- Modulation up to 3GHz (-3dB)



R. Paiella *et al.*, Appl. Phys. Lett. 77, 169 (2000)
R. Paiella *et al.*, Appl. Phys. Lett. 76, 2526 (2001)

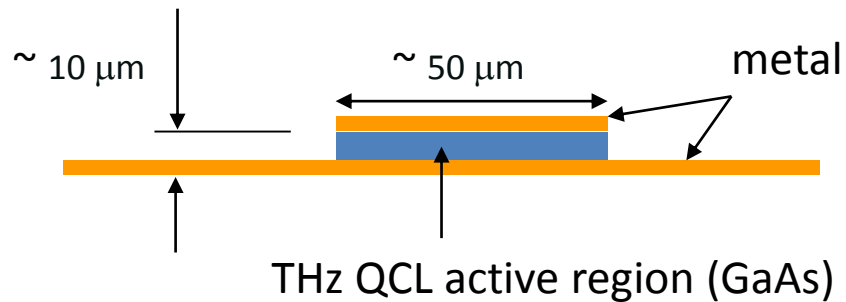
- Modulation bandwidth limited by RC time constant ($C \sim 10 \text{ pF}$)
- Number of sidebands increases significantly at the roundtrip

THz quantum cascade laser

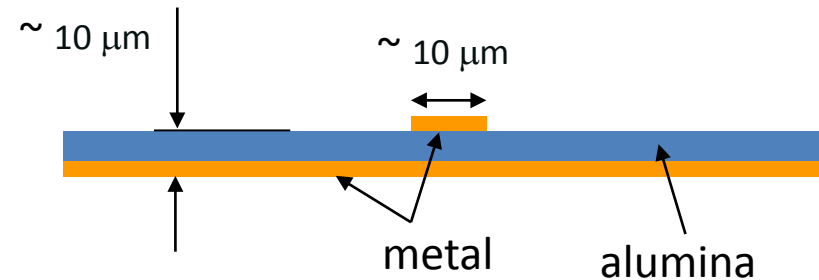


THz Waveguide and μ -wave transmission line

→ MM THz QCL waveguide



→ Thin-film μ -wave micro-strip line



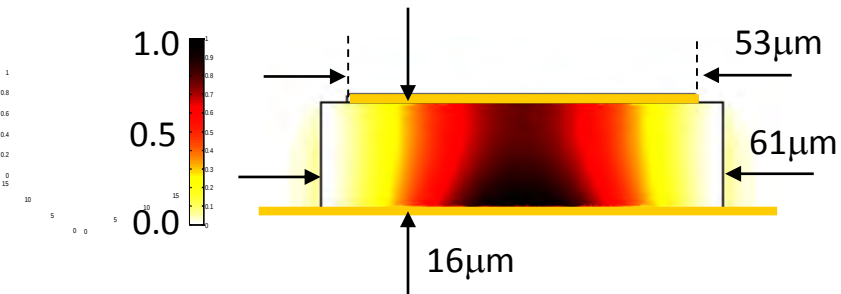
Main differences

- Dielectric: doped heterostructure
- Dielectric etched on both sides

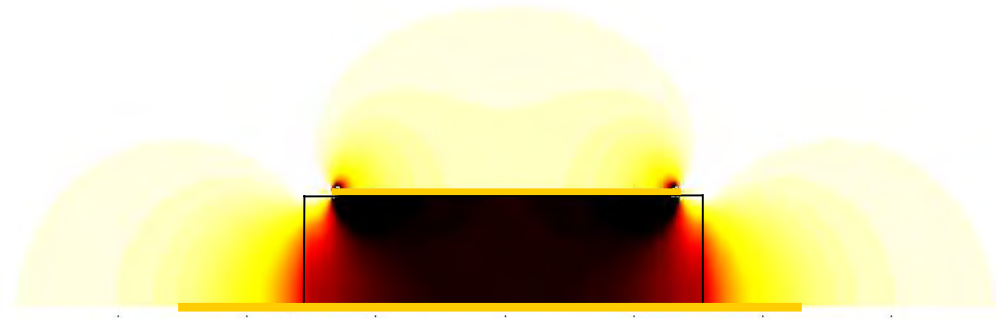
- Insulating dielectric
- Semi-infinite dielectric plane

Computed 2-D mode profiles

➤ 2.3THz

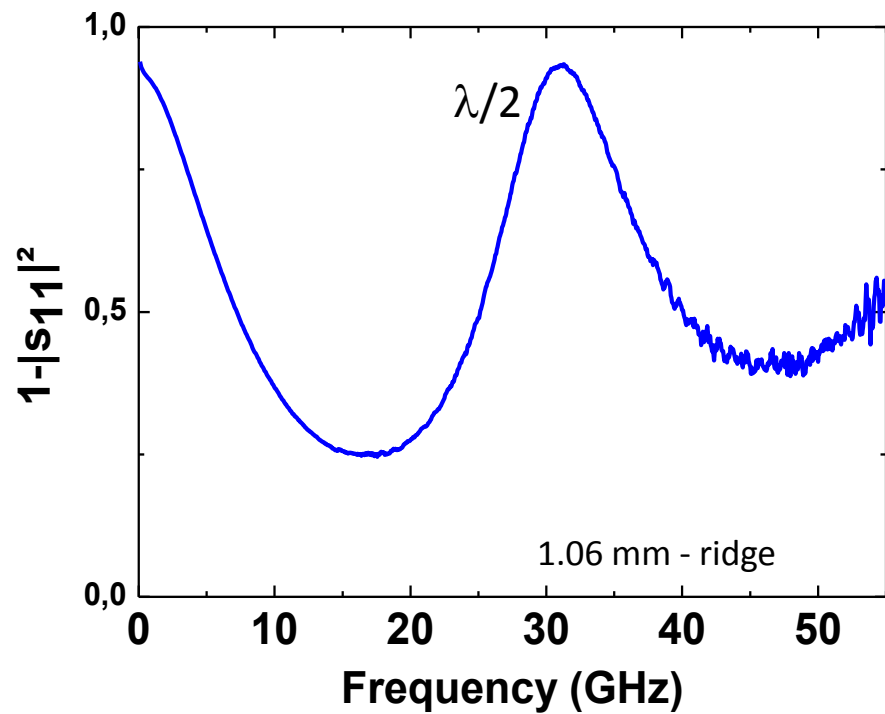
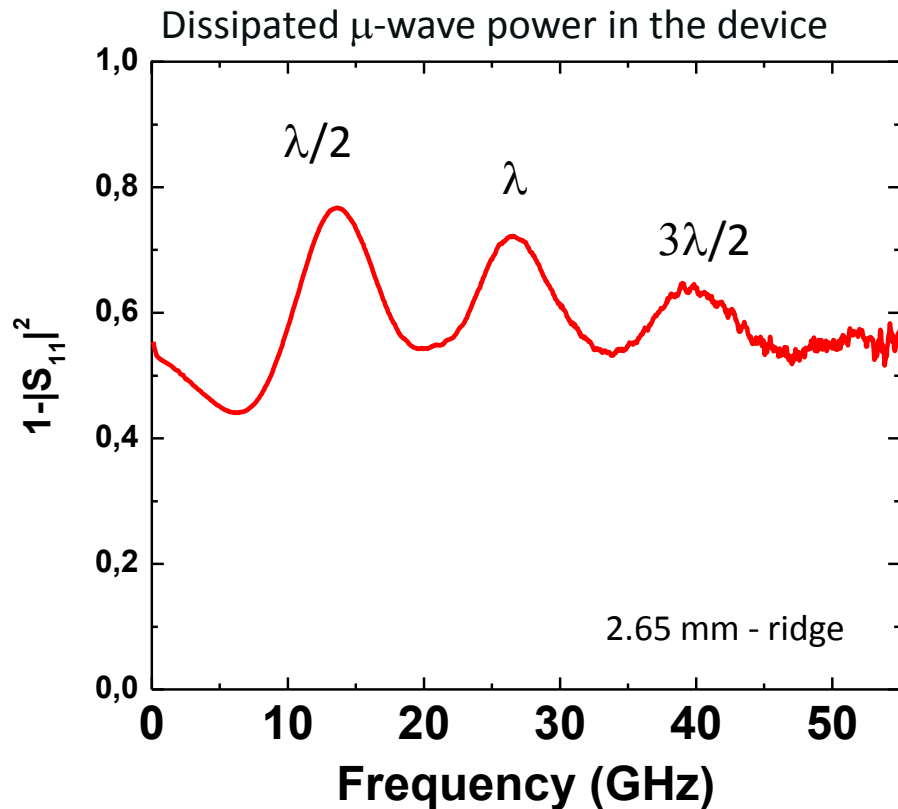
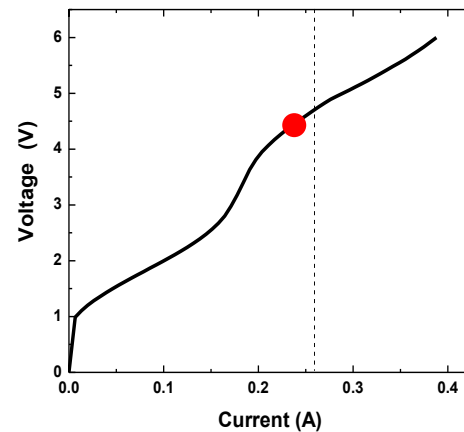
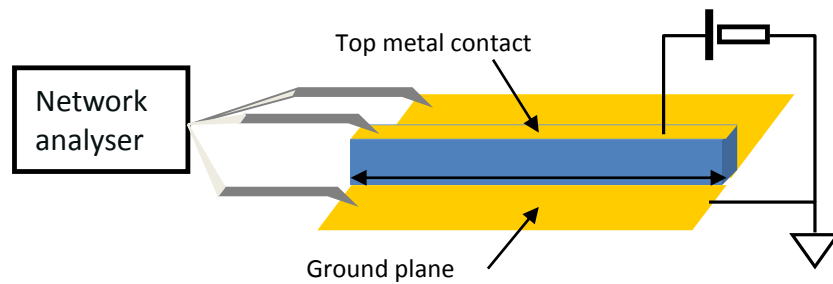


➤ 20GHz



What is the impedance of Metal-Metal THz QCL waveguides at microwave frequencies?

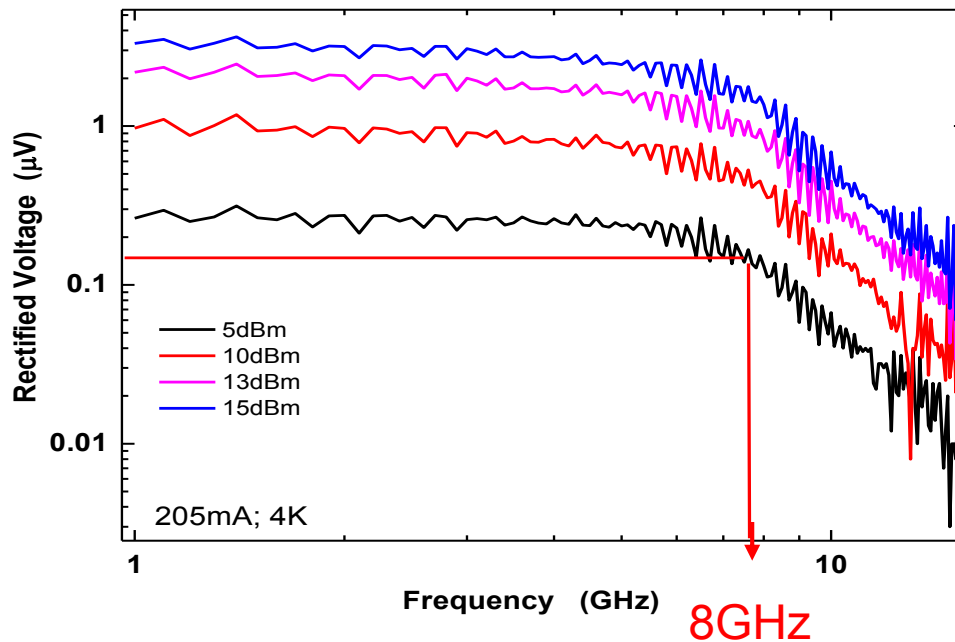
Impedance measurements



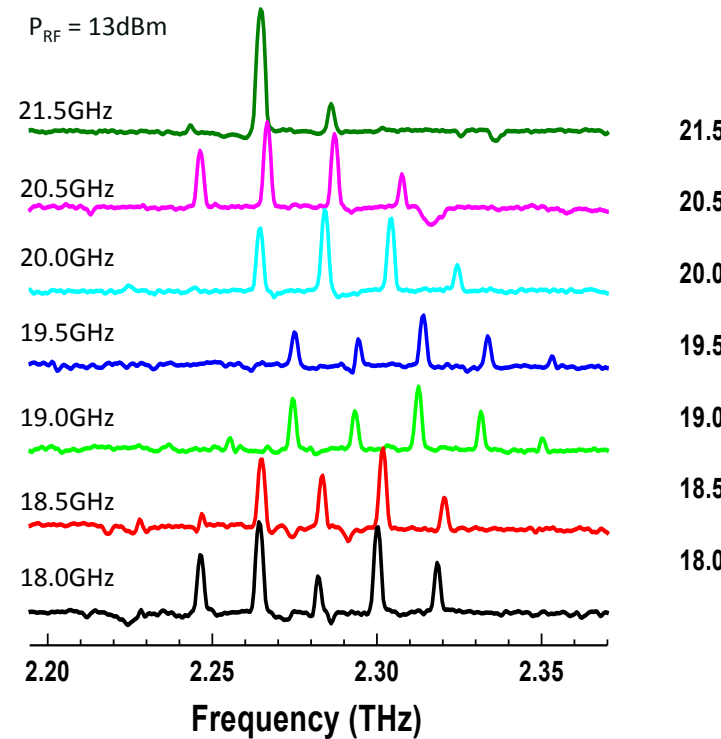
Modulation of THz- QC lasers

S. Barbieri *et al.*, Appl. Phys. Lett. (2007)

W. Maineault *et al.*, Appl. Phys. Lett. (2010)



Modulation up to > 20 GHz
using a shunt-stub matching

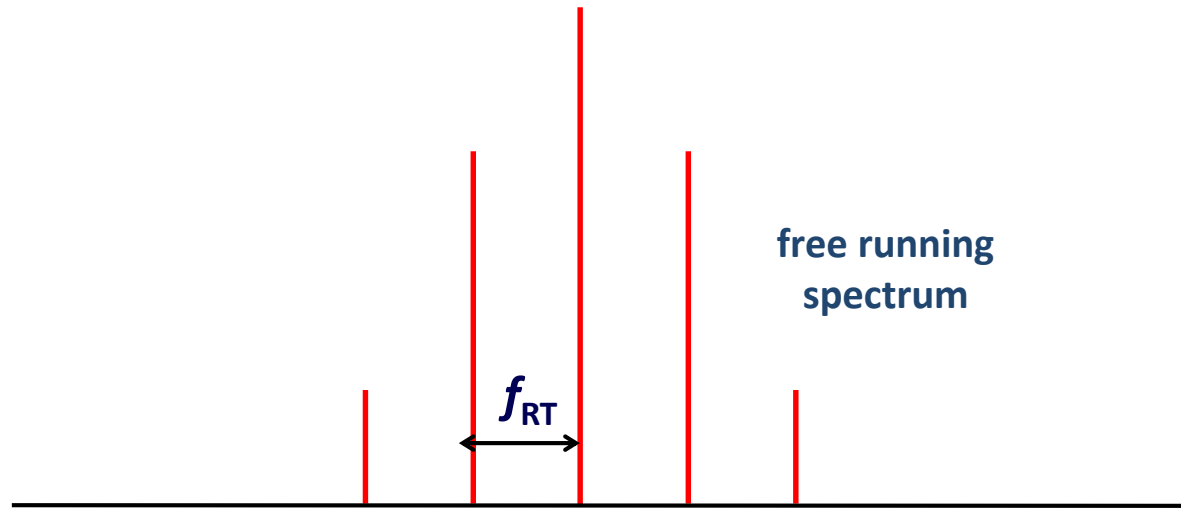


Band pass limited by our microwave circuits

Intermodal (*round-trip*) injection locking @ THz

Phase locking on a mode only...

$$f_{\text{RT}} = 10 - 50 \text{ GHz}$$



How to stabilize f_{RT} the round trip frequency

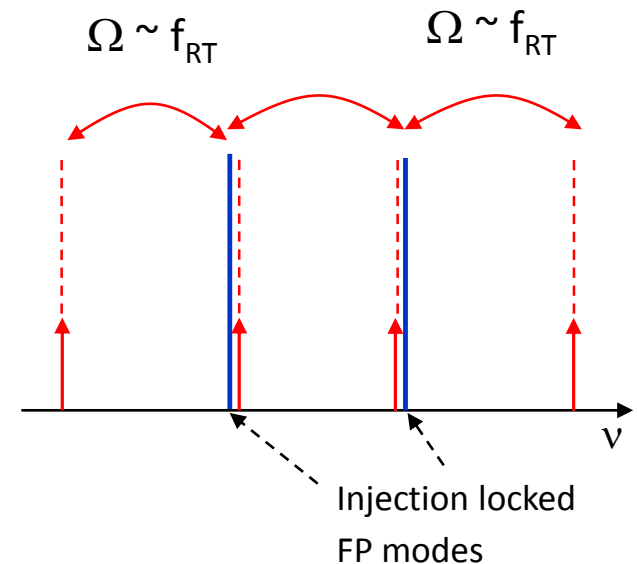
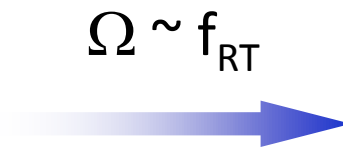
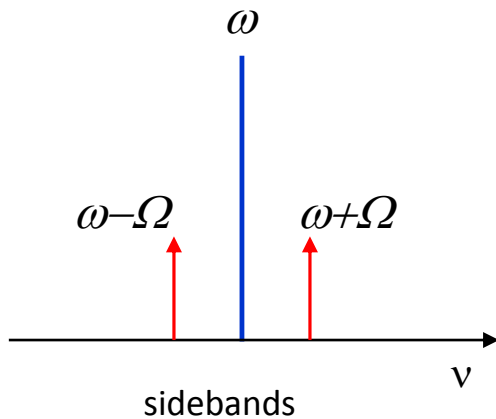
Amplitude modulation

Amplitude modulation at frequency Ω :

Monochromatic lasers $E \cos(\omega t + \phi)$

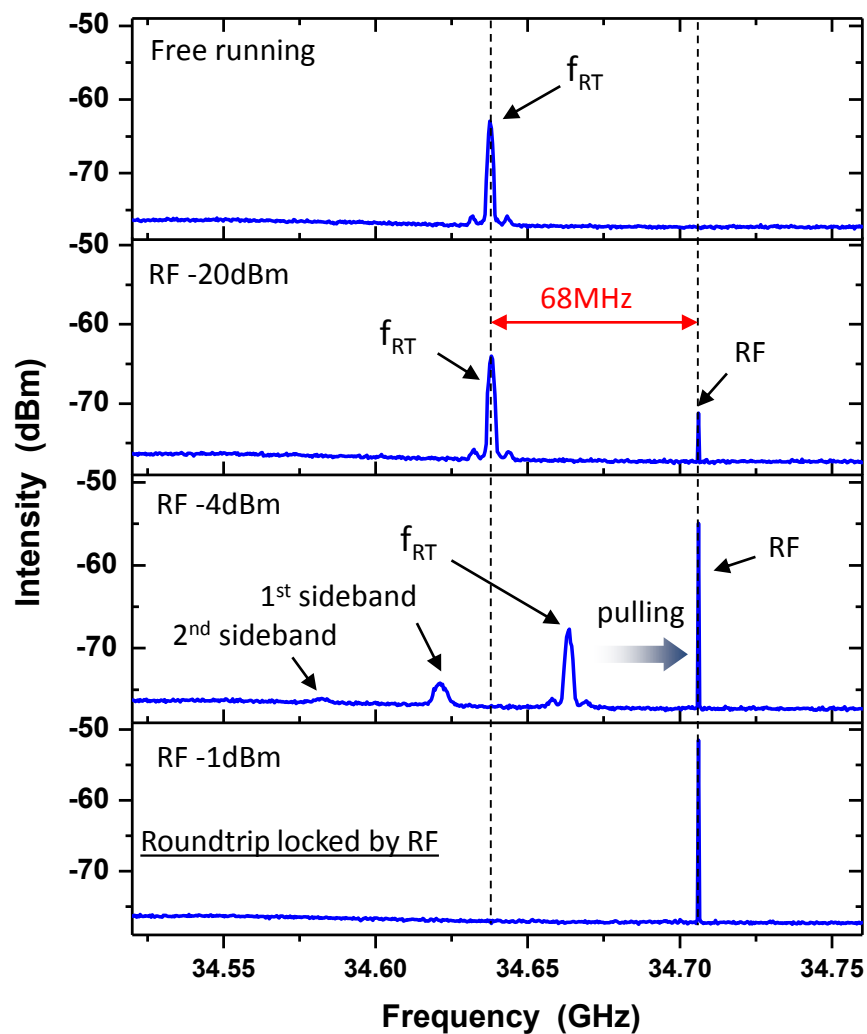
Modulation at Ω of the laser $(E \sin(\omega t + \phi)) (A + B \cos(\Omega t)) =$

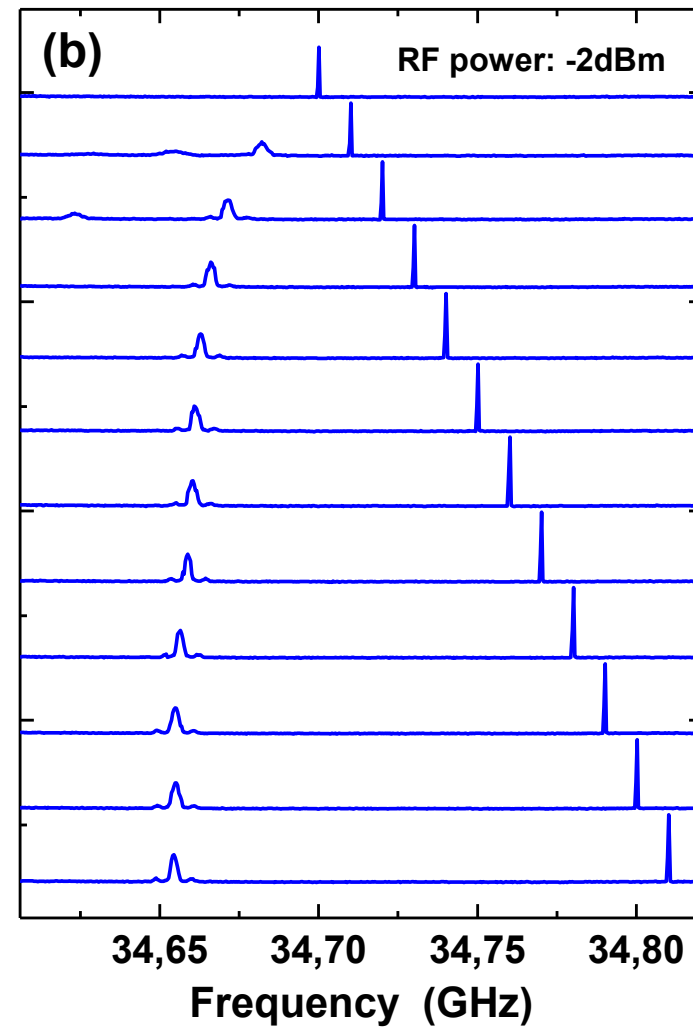
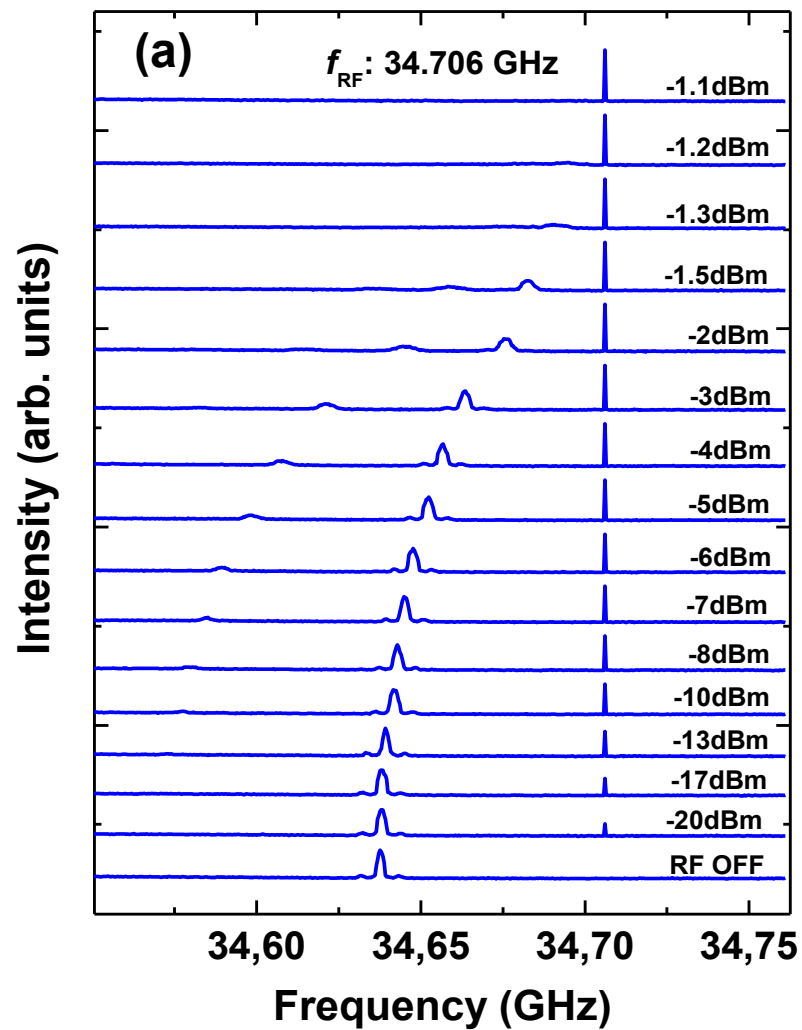
$$= \frac{BE}{2} \sin((\omega + \Omega)t + \phi) + \sin((\omega - \Omega)t + \phi) + AE \sin(\omega t + \phi)$$



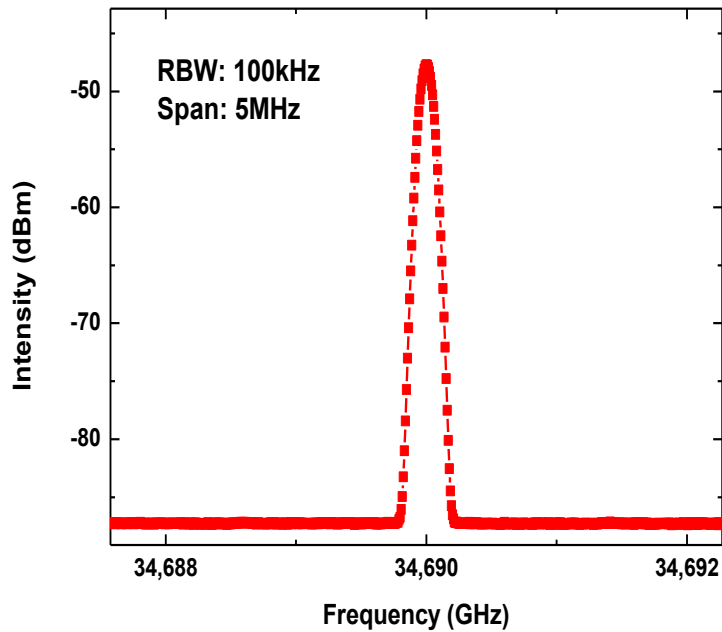
Intermodal injection locking at 34.7GHz

1.3mm long laser $\rightarrow$ Injection at $\sim 35\text{GHz}$!

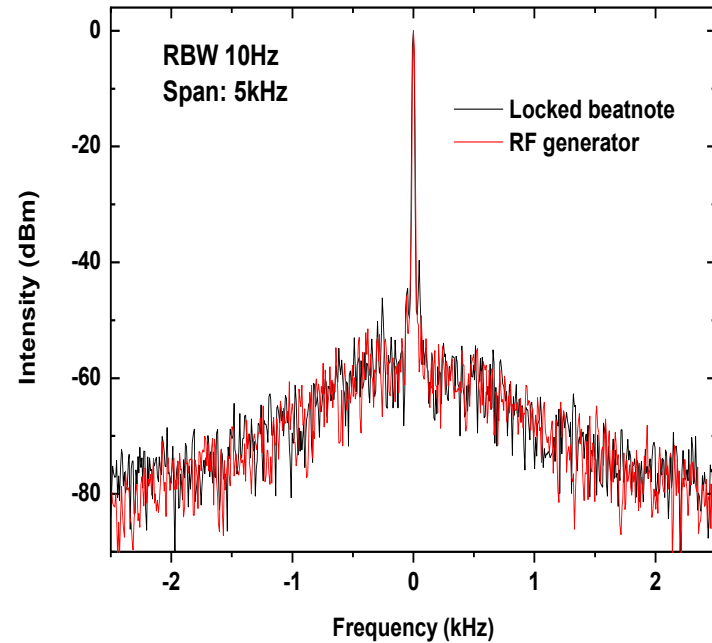




Locked beat-note linewidth



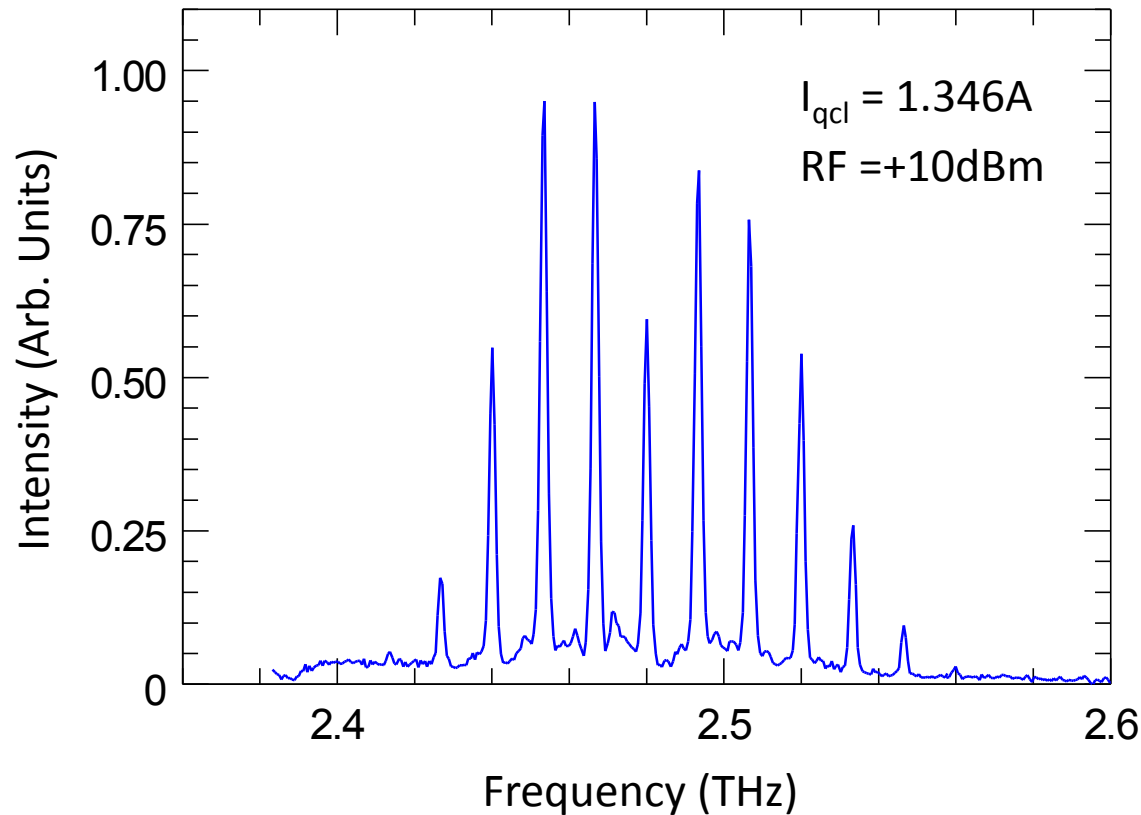
Free running



Locked

Injected optical spectrum

The spectrum has several modes due to the RF injection at the round trip

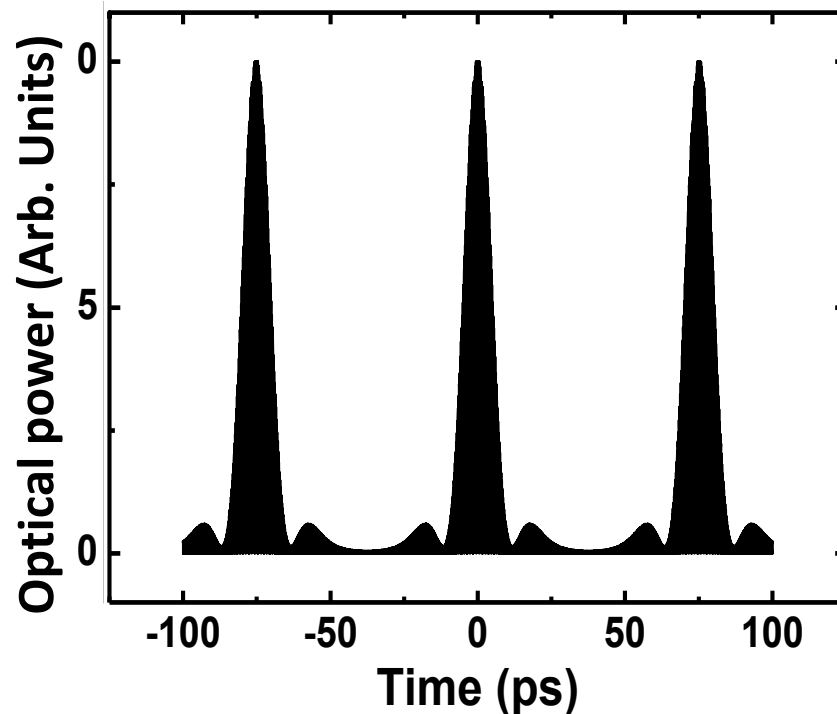


S. Barbieri *et al.* Nature Photon. **5**, 306 (2011)

C. Sirtori, *et al.* Nature Photon. **7**, 691 (2013)

Coherent detection of THz QC laser mode-locking

- Active THz QCL mode-locking measured by an asynchronous optical sampling



Pulse width: **10ps**

- Measured pulse train
- Pulse train **calculated by supposing** a negligible phase dispersion (*transform limited pulses*)

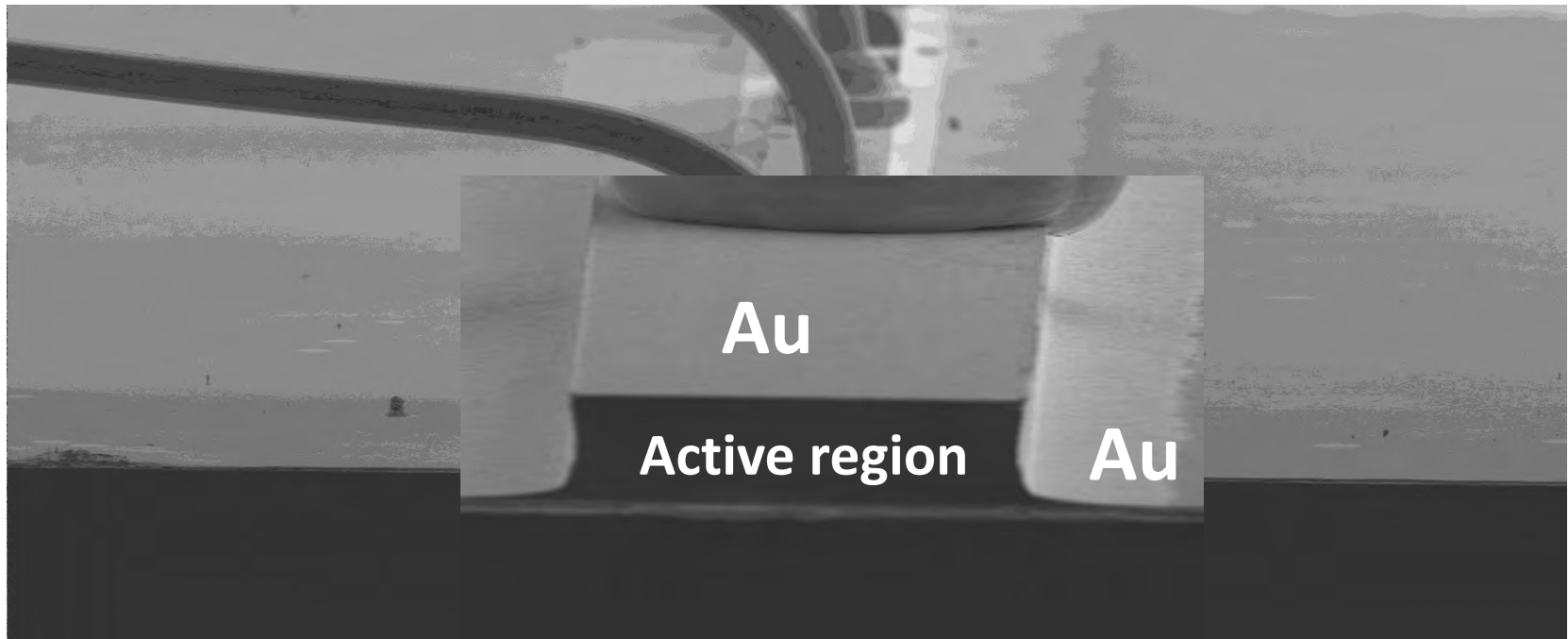
S. Barbieri *et al.* Nature Photon. **5**, 306 (2011)

C. Sirtori, *et al.* Nature Photon. **7**, 691 (2013)

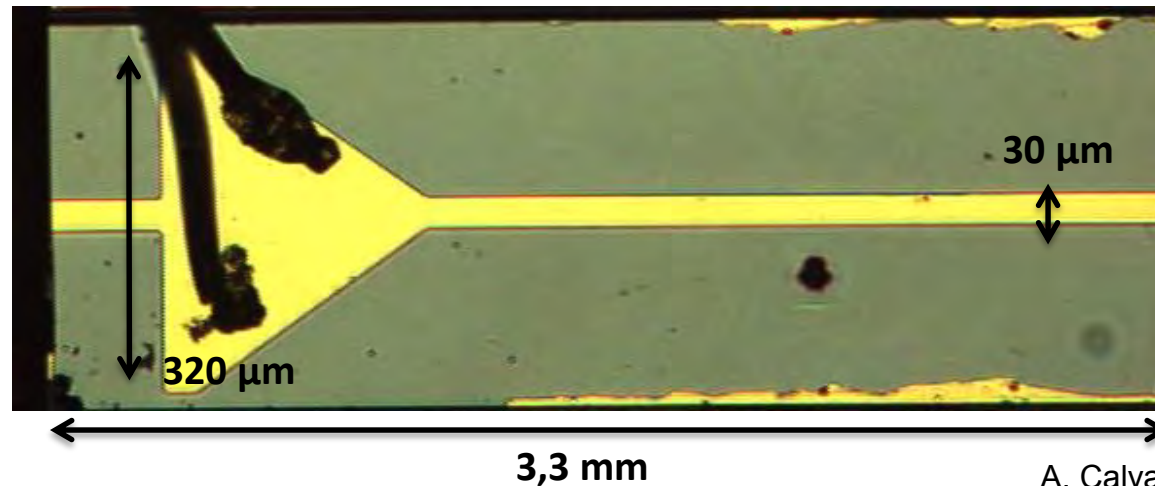
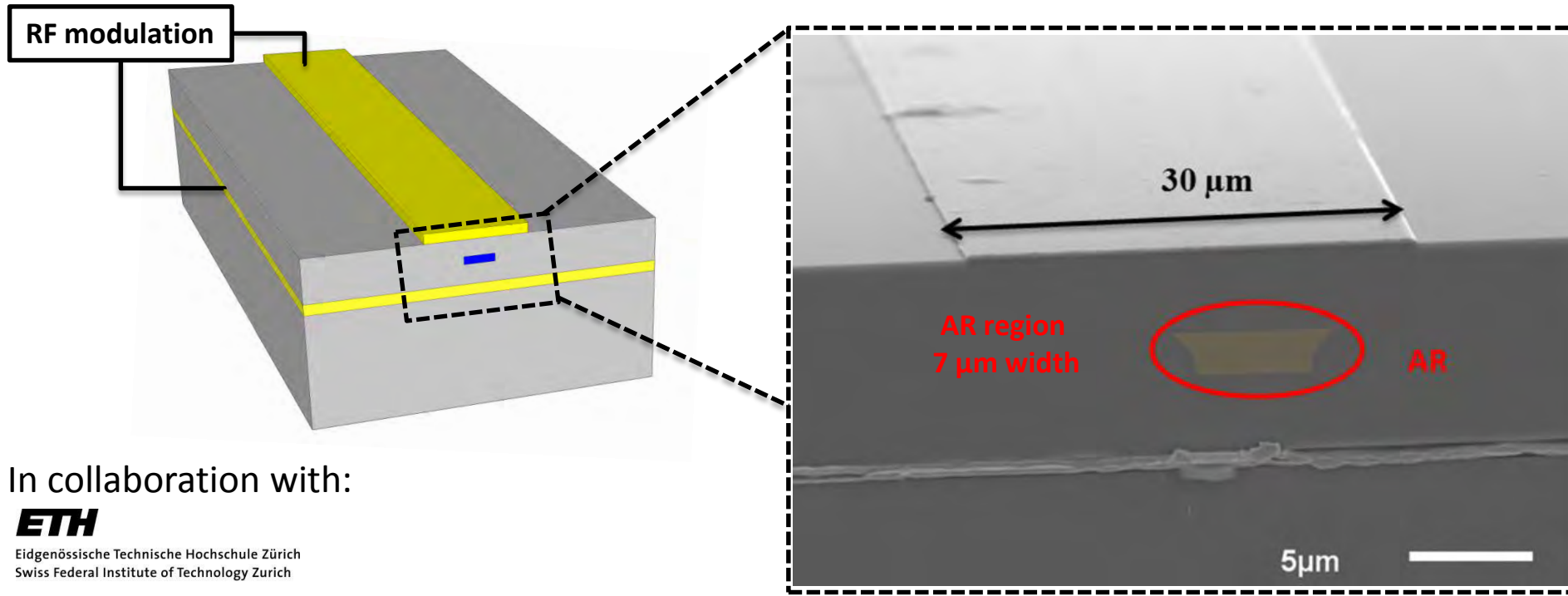
Intermodal (*round-trip*) injection locking in the mid-IR

Let us copy ! ...

THz quantum cascade laser



QC laser embedded within a microwave strip

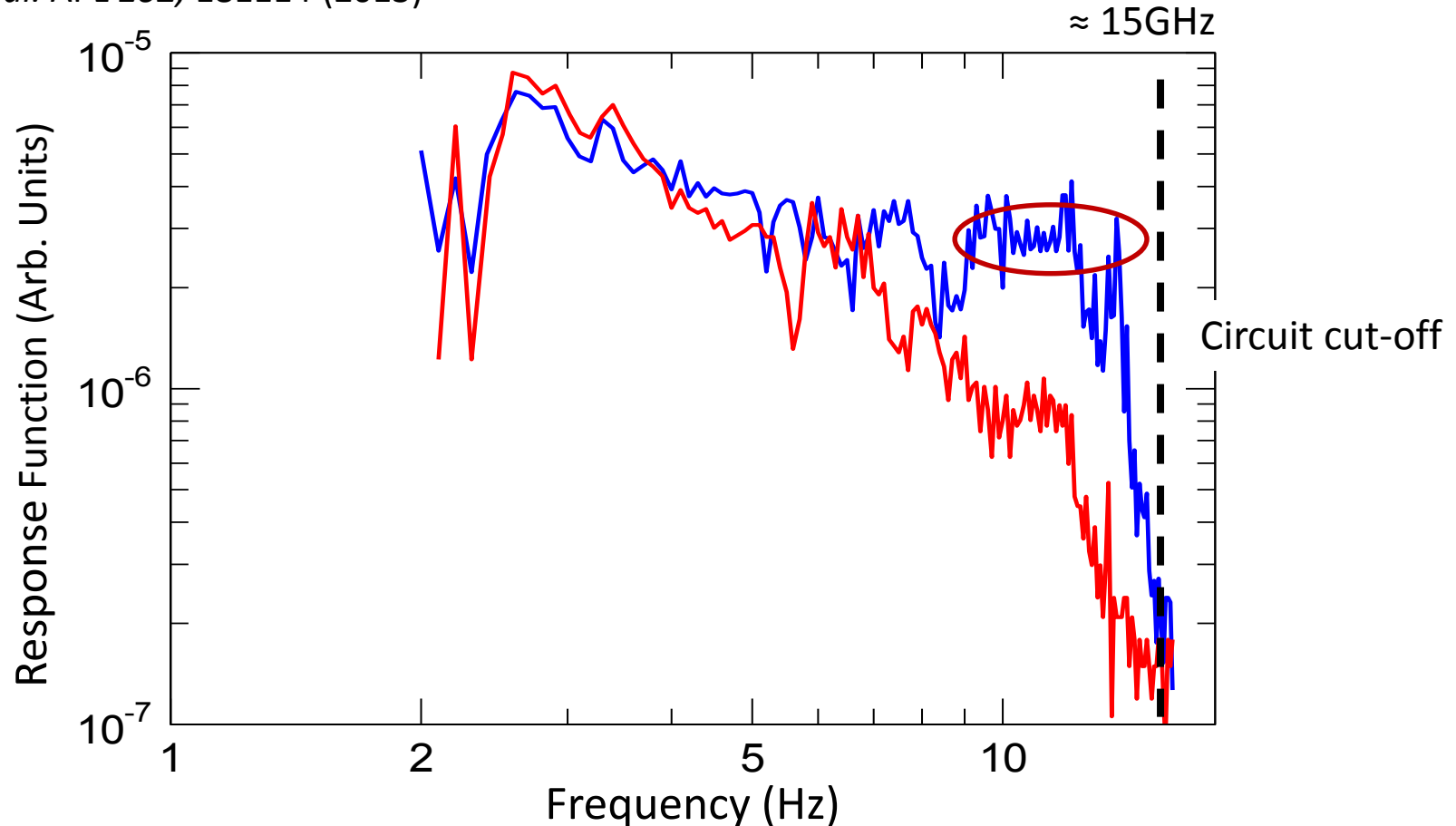


Geometry for the top contact :

→ AR not damaged by bonding

High frequency response (comparison)

Calvar et al. APL **102**, 181114 (2013)



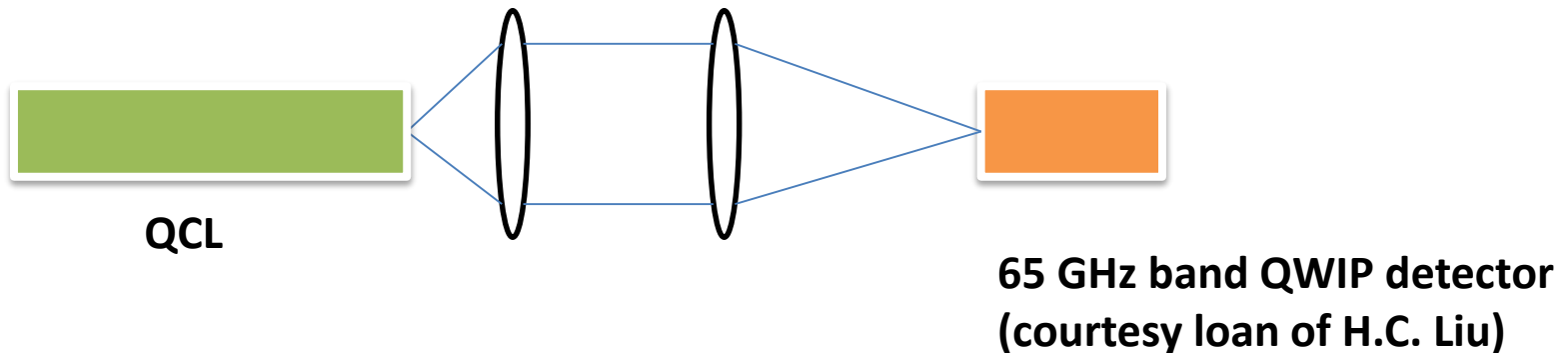
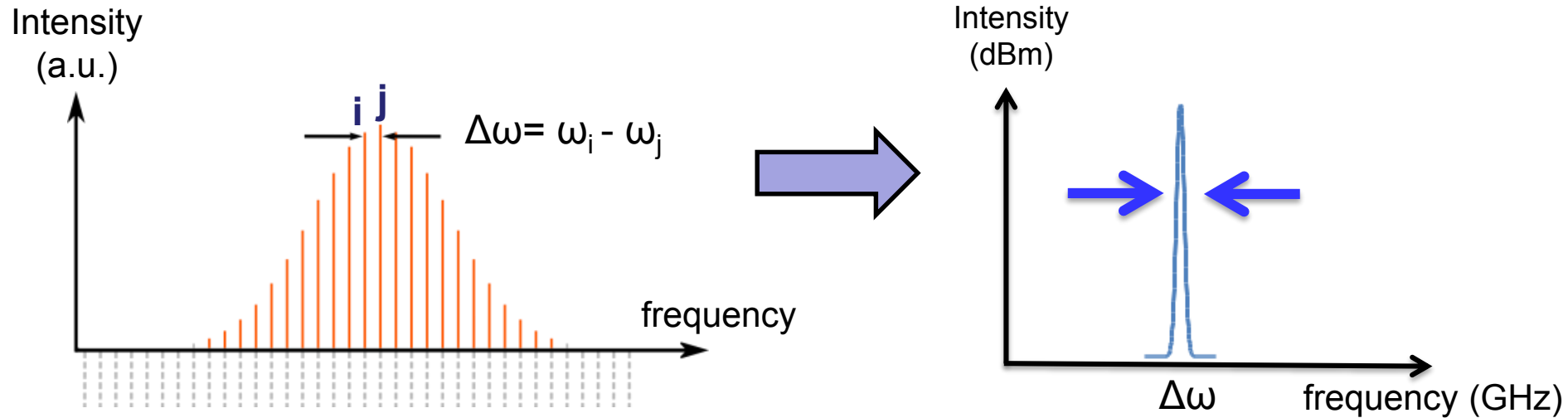
Comparison between a standard buried heterostructure (red) and the microwave-strip laser (blue)



Net improvement of the band pass up above 8GHz

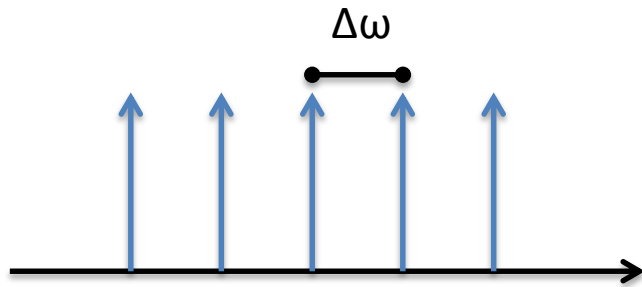
Monitoring the laser modes separation

Optical spectrum is wide in QC lasers

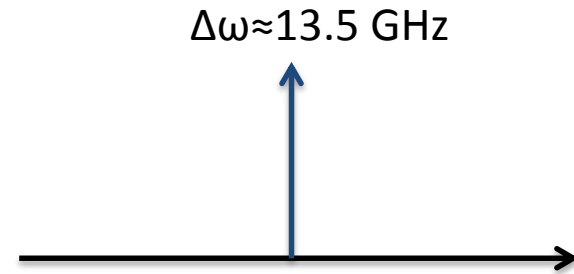


Stability of the cavity modes

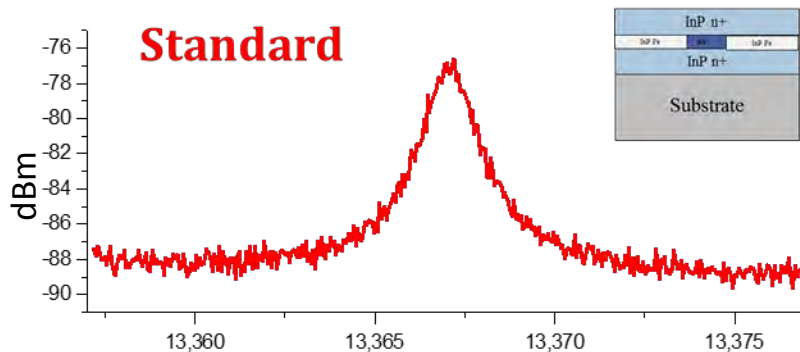
Optical spectrum :



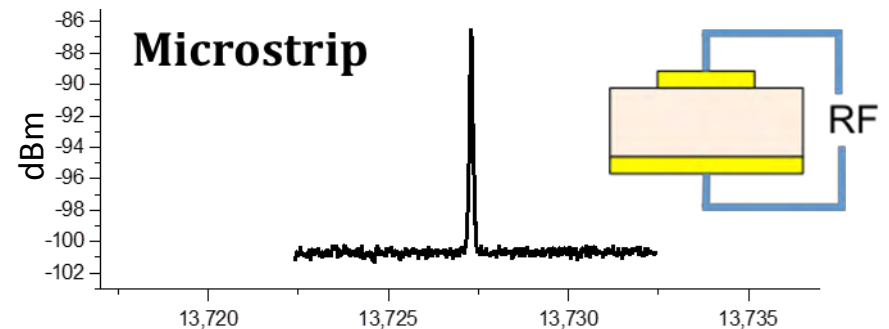
Microwave spectrum :



The shape of the beatnote gives an insight of the noise behavior of the laser modes



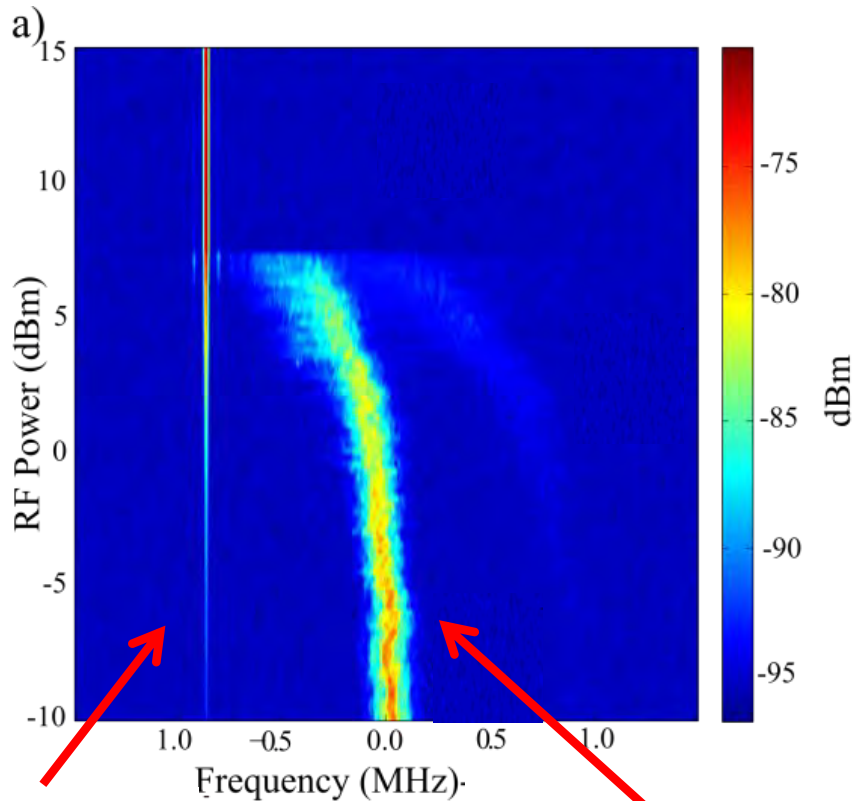
FWHM 1,3 MHz



FWHM 100 kHz

Beat note injection experimental data in the Mir

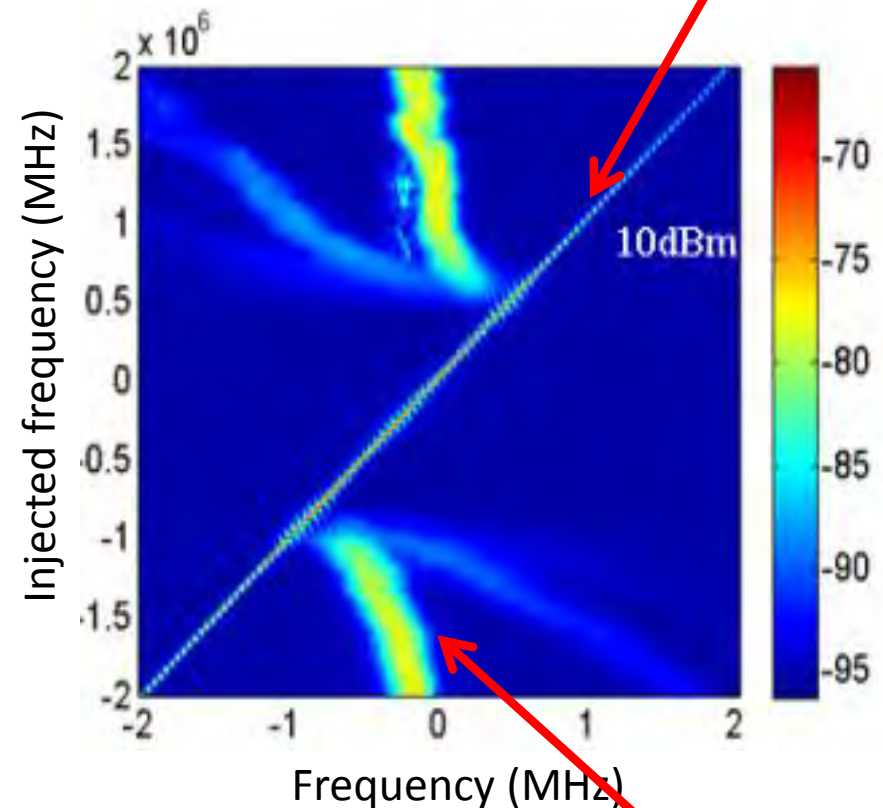
Power injection



Injected microwave

Beating between the longitudinal modes

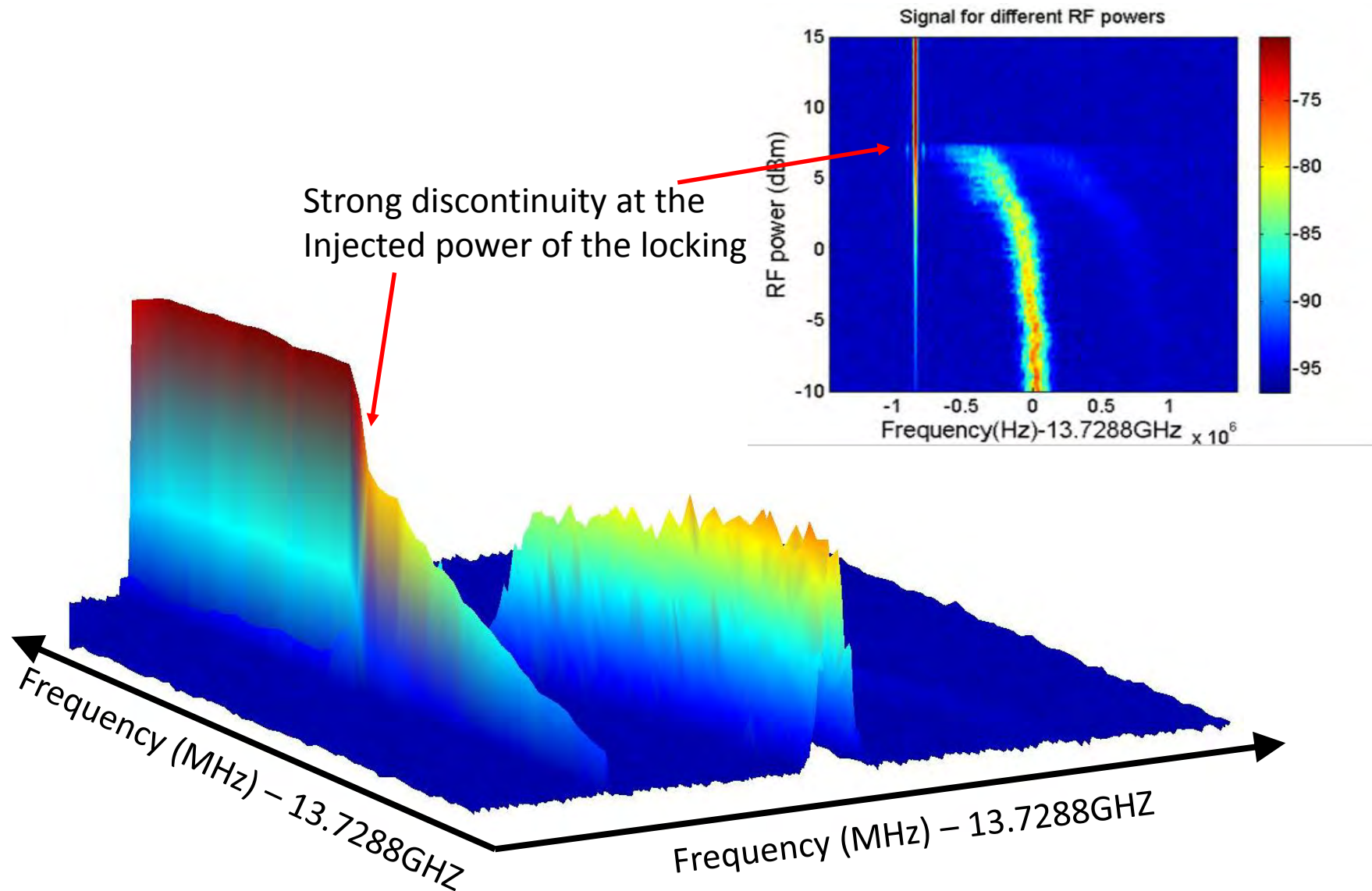
Frequency injection



Injected microwave

Beating between the longitudinal modes

Beat note injection experimental data in the Mir



Mid-Infrared pulses?

No pulses have been measured!

(we have used a second order correlation using a two photon QWIPA)...

What is the difference between MIR and THz devices:

In the THz the upper state the lifetime can much longer than in the mid infrared

- @ THz (bound to continuum) $\sim 10 - 20\text{ps}$
- @MIR $\sim 0.5 - 1\text{ps}$

Mode-locking of QCLs

ARTICLES

PUBLISHED ONLINE: 24 APRIL 2011 | DOI: 10.1038/NPHOTON.2011.49

nature
photonics

Coherent sampling of active mode-locked terahertz quantum cascade lasers and frequency synthesis

Barbieri *et al.* Nature Photon. **5**, 306 (2011)

J. Freeman *et al.* OPEX. **21**, 16162 (2013)

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13 DECEMBER 2012 | VOL 492 | NATURE | 229

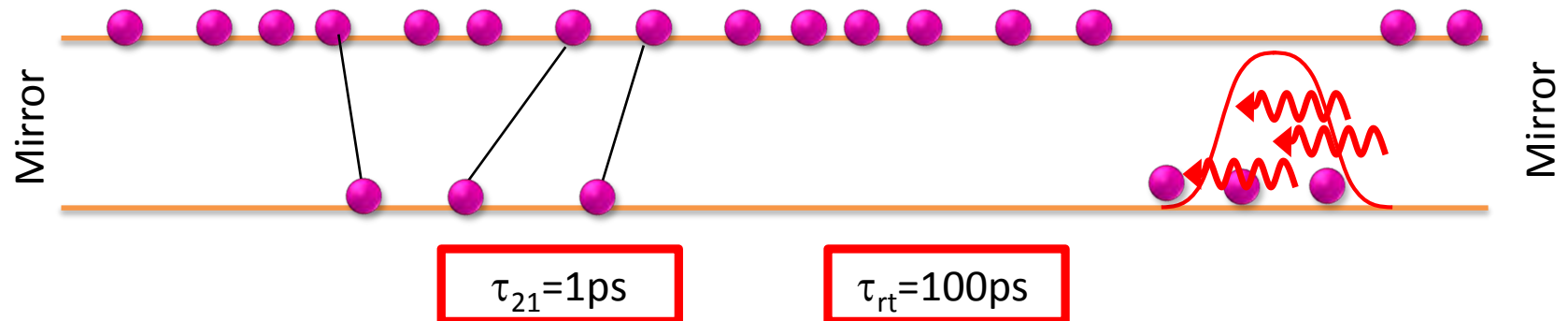
doi:10.1038/nature11620

Tomorrow talk of J. Faist

Mid-infrared frequency comb based on a quantum cascade laser

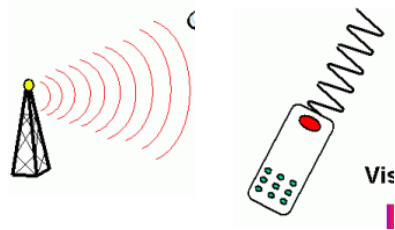
Andreas Hugi¹, Gustavo Villares¹, Stéphane Blaser², H. C. Liu³ & Jérôme Faist¹

System not favourable for pulse generation
→ phase relation arising from FM

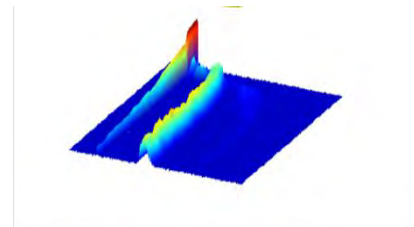


Conclusions

- Modulation of QC lasers has been measured above 30GHz



- QC lasers embedded in double metal waveguides can be easily injected at the round trip frequency and can give rise to frequency combs without generating pulses



- Mode-locking of QC lasers seems possible only if the lifetime exceeds tens of ps

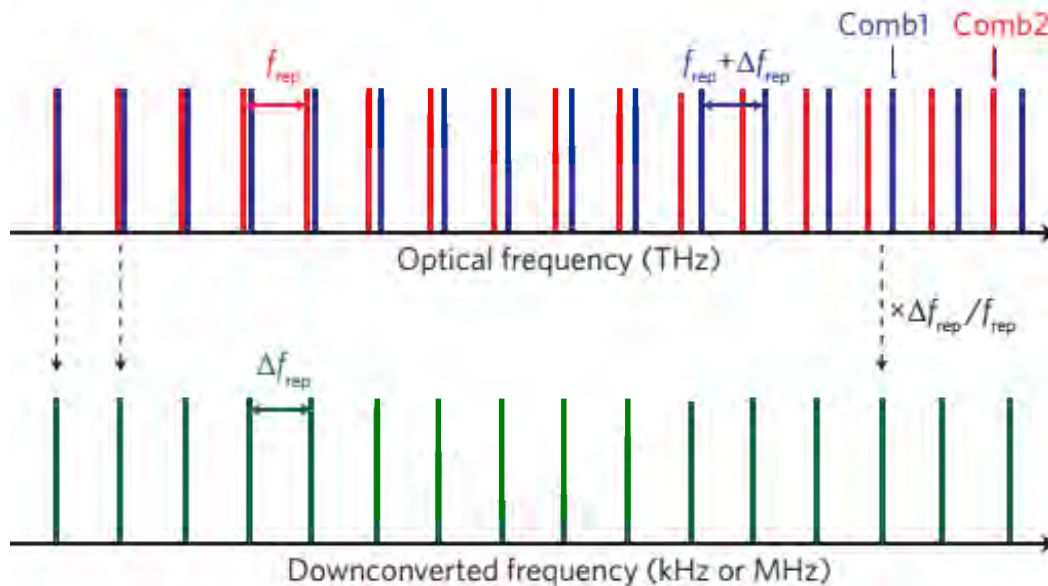
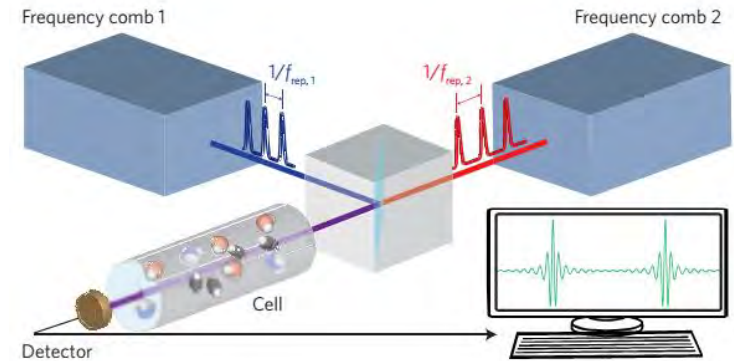
Frequency Comb Spectroscopy

Dual comb spectroscopy:

2 lasers with two different repetition rates



2 combs slightly different mode separation



Optical spectrum

Microwave

- The optical absorption spectrum is mapped into the radiofrequency domain